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The operational DMI-HIRLAM system
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The Operational HIRLAM System at DMI - October 1999 -

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1. Introduction

A numerical weather prediction system “DMI-HIRLAM” is run operationally at the Danish Meteorological Institute (DMI). The goal of the DMI weather prediction system is to provide high accuracy meteorological forecast products, with a special priority on forecasts valid for the short range, up to about two days ahead. The system provides guidance to both meteorological staff (forecasters) and to numerous customers in general. Furthermore, the results are used as input (forcing) to specialized forecasts (e.g., a storm surge model and a road conditions model).

HIRLAM stands for HIgh Resolution Limited Area Model. This implies that the physical laws of the atmosphere expressed in mathematical form are transformed to numerical schemes operating on a system of grid points resolving the 3-dimensional space in high resolution, that is, with a short geographical distance between the model grid points. The model forecasts are carried out on a large computer system.

The DMI operational forecasting system originates from the international HIRLAM project (Machenhauer, 1988; Gustafsson, 1993; Källén, 1996). This collaboration started back in 1985 and has continued since then. The national meteorological institutes of Sweden, Spain, Norway, Ireland, Iceland, Holland, Finland and Denmark participate in the development of the forecasting system. Since 1992 Météo-France has been an associated partner. Although most components in the operational forecasting systems come from the international collaboration the implementations differ among the HIRLAM countries because of differences in computer facilities and various technical strategies chosen.

The DMI system involves several nested models and large integration domains (see Appendix A). The biggest HIRLAM model area needs boundary values evolving in time from an external model (the host model). In this case the host model is operated by the ECMWF (European Centre for Medium-Range Weather Forecasts). The inner models, in turn, receive their boundary values from the associated HIRLAM host model. The model forecasts need to start from realistic initial states of the atmosphere. This requires the processing of observations in a suitable data-assimilation system. The success of a numerical weather prediction system is governed by the quality of the forecast model in combination with the methodology for assimilating observations.

The main priority of the present report is to document the physical principles and the mathematical equations behind the DMI-HIRLAM forecast model. Numerical aspects of the model are included to some extent. Technical implementation details related to computers and model codes are not covered by the present report.

The model dynamics are described in section 2. This description concerns not only the continuous equations for atmospheric motion, but also numerical aspects including the question of coupling the model adiabatic processes with the diabatic processes (physical parameterizations). Information on the model grid used for the numerical computations is given in Appendix B.

The atmospheric physics are described in section 3. The key processes (radiation, turbulence, condensation and convection with precipitation release) are treated, including also a description of parameterization problems associated with each process. Appendix C contains information on some details in the model computation of atmospheric longwave radiation.

The surface treatment is covered by section 4. At first, a description of the surface fluxes of heat, moisture and momentum over different surface types is provided. Secondly, the surface energy and moisture budget is described including prediction equations for soil variables. Finally, the generation of physiographic data is mentioned. These data, provide the necessary information to assess the lower atmospheric boundary condition.

The system for assimilating observational data (the analysis system) is briefly outlined in section 5. The operational use of the data assimilation system is described in Appendix A, which contains information on operational data processing, geographical areas for the different model versions, and a table with key parameters of the operational setup.

Finally, important diagnostic measures of practical significance are described in section 6.

2. Model dynamics

From a physical and a mathematical point of view the behavior of the atmosphere is governed by the equations of motion, the equation of continuity for atmospheric constituents including moisture variables, the equation of state and the first law of thermodynamics. In addition, for the present hydrostatic model, the hydrostatic relation between increments of geopotential and pressure is utilized. The equations should include forcing terms comprising sources and sinks. Also the appropriate boundary conditions must be specified. For a Limited Area Model not only the lower and the upper boundary conditions are needed but also the lateral boundary conditions. The continuous equations are described in section 2.1.

In formulating a numerical model many considerations are needed on how to solve the atmospheric modeling problem. This is because the equations of motion allow for a rich variety of phenomena, and the numerical schemes used are crucially important for the quality and success of the model.

The present model dynamics are based on finite differences. The model grid (horizontal) is shown in Appendix B. The dynamics is of Eulerian type. In order to allow for

reasonably long time steps the computations are split into an ‘explicit part’ and a ‘semi-implicit part’ (subsection 2.2). The latter takes care of the fast gravity wave terms such that the numerical stability criterion is governed by the meteorologically significant advection (CFL criterion).

In order to prevent accumulation of energy of the smallest scales a horizontal diffusion is required. For the current model resolutions this is utilized mainly for numerical reasons. Only for a very high resolution, resolving partly the turbulence, the horizontal diffusion will represent effects of horizontal turbulence. The horizontal diffusion currently used in HIRLAM is briefly described in subsection 2.3.

The lateral boundary condition represents a dynamical forcing which needs to be treated in a realistic way. The current methodology (boundary relaxation) is described in subsection 2.4. Three time levels of the forecast variables are available, and the time stepping is done by the *leapfrog* method (Haltiner, 1971). A time filter connecting even and odd time steps is described in subsection 2.5. The complete time stepping strategy including also the physical parameterizations is described in subsection 2.6. The model formulation allows for different time steps used for the dynamical processes and the physical parameterizations, respectively.

2.1. The continuous equations

The dynamical equations are solved for a general pressure based and terrain following coordinate $\eta(p, p_s)$. p is pressure and p_s is the surface pressure

$$\eta(0, p_s) = 0$$

and

$$\eta(p_s, p_s) = 1$$

The model is derived for a spherical coordinate system (λ, θ) , but in the formulation two metric coefficients h_x, h_y have been introduced. For a distance $\delta X, \delta Y$ on the earth, with radius a , this yields

$$\delta X = ah_x \delta x$$

and

$$\delta Y = ah_y \delta y$$

Currently the HIRLAM model uses spherical rotated coordinates giving

$$\delta X = a \cos \theta \cdot \delta \lambda$$

and

$$\delta Y = a \delta \theta$$

The atmospheric forecast variables defined in three dimensions are the horizontal wind components u and v , surface pressure p_s , temperature T , specific humidity q , specific

cloud condensate q_c and turbulent kinetic energy E . In the equations below, the forcing term for variable γ due to other processes than dynamics is called F_γ . The lateral boundary conditions are disregarded at this stage.

The momentum equations are

$$\frac{\partial u}{\partial t} = (f + \xi)v - \dot{\eta} \frac{\partial u}{\partial \eta} - \frac{R_d T_v}{ah_x} \frac{\partial \ln(p)}{\partial x} - \frac{1}{ah_x} \frac{\partial(\phi + E_m)}{\partial x} + F_u \quad (1)$$

$$\frac{\partial v}{\partial t} = -(f + \xi)u - \dot{\eta} \frac{\partial v}{\partial \eta} - \frac{R_d T_v}{ah_y} \frac{\partial \ln(p)}{\partial y} - \frac{1}{ah_y} \frac{\partial(\phi + E_m)}{\partial y} + F_v \quad (2)$$

In (1) and (2) above

$$\xi = \frac{1}{ah_x h_y} \left(\frac{\partial(h_y v)}{\partial x} - \frac{\partial(h_x u)}{\partial y} \right)$$

and

$$E_m = \frac{1}{2}(u^2 + v^2)$$

$\dot{\eta}$ is the vertical velocity in the η -coordinate system, ϕ is the geopotential, ξ is the vorticity and E_m is the kinetic energy of the mean horizontal motion (turbulent kinetic energy is E).

For temperature the equation is

$$\frac{\partial T}{\partial t} = -\frac{u}{ah_x} \frac{\partial T}{\partial x} - \frac{v}{ah_y} \frac{\partial T}{\partial y} - \dot{\eta} \frac{\partial T}{\partial \eta} + \frac{\kappa T_v \omega}{(1 - (\delta_c - 1)q)p} + F_T \quad (3)$$

κ is the ratio between the specific gas constant and the specific heat capacity, and δ_c is the ratio between the specific heat capacity of water vapour and the corresponding value of dry air (at constant pressure). ω is the rate of pressure change following an air parcel.

For the remaining variables ($\gamma = q$, $\gamma = q_c$ and $\gamma = E$) the following advection equation applies

$$\frac{\partial \gamma}{\partial t} = -\frac{u}{ah_x} \frac{\partial \gamma}{\partial x} - \frac{v}{ah_y} \frac{\partial \gamma}{\partial y} - \dot{\eta} \frac{\partial \gamma}{\partial \eta} + F_\gamma \quad (4)$$

The hydrostatic equation takes the form

$$\frac{\partial \phi}{\partial \eta} = -\frac{R_d T_v}{p} \frac{\partial p}{\partial \eta} \quad (5)$$

and the equation of continuity is

$$\frac{\partial}{\partial \eta} \frac{\partial p}{\partial t} + \nabla \cdot \left(\vec{v}_h \frac{\partial p}{\partial \eta} \right) + \frac{\partial}{\partial \eta} \left(\dot{\eta} \frac{\partial p}{\partial \eta} \right) = 0 \quad (6)$$

The definition of the divergence operator is

$$\nabla \cdot \vec{v}_h = \frac{1}{ah_x h_y} \left(\frac{\partial}{\partial x} (h_y u) + \frac{\partial}{\partial y} (h_x v) \right) \quad (7)$$

By integrating the equation of continuity using the boundary conditions $\dot{\eta} = 0$ at $\eta = 0$ and $\eta = 1$ the equation for surface pressure tendency is obtained

$$\frac{\partial p_s}{\partial t} = - \int_0^1 \nabla \cdot \left(\vec{v}_h \frac{\partial p}{\partial \eta} \right) d\eta \quad (8)$$

The equation for pressure vertical velocity is

$$\omega = \frac{\partial p_s}{\partial t} + \int_\eta^1 \nabla \cdot \left(\vec{v}_h \frac{\partial p}{\partial \eta} \right) d\eta + \vec{v}_h \cdot \nabla p \quad (9)$$

and the equation for $\dot{\eta}$

$$\dot{\eta} \frac{\partial p}{\partial \eta} = \left(1 - \frac{\partial p}{\partial p_s} \right) \frac{\partial p_s}{\partial t} + \int_\eta^1 \nabla \cdot \left(\vec{v}_h \frac{\partial p}{\partial \eta} \right) d\eta \quad (10)$$

2.2. Semi-implicit scheme

A description of the finite difference form of the adiabatic equations above has been made (Källén, 1996), see also (Simmons and Burridge, 1981). Following the work of (Arakawa, 1966) and (Sadourny, 1975), the scheme has been designed to preserve, in a global model, several important integral constraints associated with the continuous equations, e.g., the conservation of mass.

The pressure at the coordinate surfaces (half levels) are given from the following expression using predefined coefficients $A_{k+\frac{1}{2}}$ and $B_{k+\frac{1}{2}}$, ($k=0, \dots, N$), where:

$$p_{k+\frac{1}{2}} = A_{k+\frac{1}{2}} + B_{k+\frac{1}{2}} p_s \quad (11)$$

In (11) the coefficients $A_{k+\frac{1}{2}}$ and $B_{k+\frac{1}{2}}$ are currently chosen such that $B_{k+\frac{1}{2}} = 0$ for the uppermost levels (pressure coordinate surfaces) while $A_{k+\frac{1}{2}} = 0$ near the ground (terrain following coordinates).

The finite differences are second order accurate and the horizontal grid is an Arakawa C grid (see Appendix B).

The preliminary updates from the dynamics are written in the following form using a *leapfrog* time step

$$u_{n+1}^* = u_{n-1} + 2\Delta t \left(\frac{\partial u}{\partial t} \right)_{e,n} - \frac{1}{ah_x} \delta_x \left(\frac{1}{2} \Delta_{tt} P \right) \quad (12)$$

$$v_{n+1}^* = v_{n-1} + 2\Delta t \left(\frac{\partial v}{\partial t} \right)_{e,n} - \frac{1}{ah_y} \delta_y \left(\frac{1}{2} \Delta_{tt} P \right) \quad (13)$$

$$T_{n+1}^* = T_{n-1} + 2\Delta t \left(\frac{\partial T}{\partial t} \right)_{e,n} - \frac{1}{2} \tau \Delta_{tt} d \quad (14)$$

$$\ln p_{s,n+1}^* = \ln p_{s,n-1} + 2\Delta t \left(\frac{\partial \ln p_s}{\partial t} \right)_{e,n} - \frac{1}{2} \nu \Delta_{tt} d \quad (15)$$

In the equations above the first term on the right hand side is the prognostic variable at the old time step, the second term is an explicit term using the dynamical equations described in the previous section. The third term of each equation is a semi-implicit term included to treat gravity wave terms in such a way that the time step allowed to retain numerical stability in the model is determined by the advection terms. Let γ be an arbitrary parameter. The following definitions apply:

$$\begin{aligned}\delta_t(\gamma) &= \frac{(\gamma_{n+1} - \gamma_{n-1})}{2\Delta t} \\ P &= \chi T + R_d T_r \ln p_s \\ d &= \nabla \cdot \vec{v}_k\end{aligned}$$

The matrices χ , τ and ν include constants in the vertical discretization. A linearization is done about a constant reference temperature T_r and surface pressure p_r . Further details of the semi-implicit scheme have been documented, (Källén, 1996). For the additional prognostic variables (q , q_c and E) corresponding dynamical updates are used, but excluding a semi-implicit correction term.

2.3. Horizontal diffusion

A linear fourth order horizontal diffusion scheme is applied on the preliminary updated values of the forecast parameters after the explicit and the semi-implicit updates. The increment $\delta\gamma_{hd}$ to the preliminary updated values γ_{n+1}^* are

$$\delta\gamma_{hd} = \gamma_{n+1}^* - \Delta t K_\gamma \nabla^4 \gamma_{n+1}^* \quad (16)$$

K_γ is a diffusion coefficient depending on resolution and time step. For details see (Källén, 1996).

2.4. Lateral boundary condition

A Limited Area Model (LAM) is dependent on the forcing of the atmospheric forecast variables from the boundary conditions supplied by a host model. A distinction is made between variables supplied by the host model and variables only available in the LAM. The former type of variables are u , v , T , q and $\ln p_s$. For these variables the interior variables are adjusted towards the prescribed boundary values γ_b as a further update to the preliminary values γ_{n+1}^* at the new time step. A similar boundary relaxation strategy has been described (Davies, 1976; Källberg, 1977).

$$\gamma_{n+1} = (1 - \alpha_b)\gamma_{n+1}^* + \alpha_b\gamma_{b,n+1} \quad (17)$$

In (17) γ_b is linearly interpolated in time between boundary data sets. The boundary update frequency (new values for time interpolation) is given in Appendix A for the different operational HIRLAM versions. The default value of α_b is

$$\alpha_b = 1 - \tanh\left(j \frac{2}{M-4}\right) \quad (18)$$

where j is the number of grid points from the boundary point and M is the width of the boundary zone.

The variables currently not supplied by the ECMWF model to the large scale operational DMI-HIRLAM-G model (see Appendix A) are q_c and E . In order not to impose unrealistic values inconsistent with the interior model, a relaxation similar to that described above is applied to dynamical tendencies of the forecast variables in the boundary zone. The implementation is such that the dynamical tendency produced at the boundary is having zero weight while full weight is assigned to the inner edge of the boundary zone. On the boundary points these variables evolve as a result of the physical parameterizations only.

2.5. Time filter

Three time levels of the forecast variables are available and the time stepping is done by the *leapfrog* method (subsection 2.2). In order to suppress a possible separation of even and odd time steps when using *leapfrog* time stepping the following simple time filter is used for the forecast variable γ

$$\gamma_{fil,n} = \gamma_n + \epsilon_{fil}(\gamma_{fil,n-1} + \gamma_{n+1} - 2\gamma_n) \quad (19)$$

In the equation (19) above index ‘fil’ means a time filtered value. The time filter constant ϵ_{fil} is currently 0.05.

2.6. Time stepping

A procedure for including the forcing terms from the physical parameterizations (section 3) has not yet been described. Experimentation with the HIRLAM system shows that the method used to couple updates from dynamics and physics, respectively, is important with regard to the control of numerical noise. Also the numerical stability may be affected by the coupling method. This is because the physics and dynamics may interact strongly on the smallest scales treated by the model. The importance of the coupling has also been found in other model systems (Wedi, 1999).

In the present Eulerian model the following method for coupling has proven to be fruitful: The computation of physics is carried out less frequent than the dynamics, that is, after a series of N_{ph} dynamical time steps. Currently, (in the first model setup) $N_{ph} = 3$. This value may be increased in some model versions in the future. The time stepping is carried out in the following way (see also figure 1):

- 1) A complete model state is saved, formally valid at time level $n - 1$.
- 2) The model dynamics is then run adiabatically for N_{ph} time steps using the *leapfrog* time stepping as described in subsection 2.2. Also the horizontal diffusion (subsection 2.3), the boundary relaxation (subsection 2.4) and the time filter (subsection 2.5) is applied every dynamical time step Δt which is finalized by a swapping

(renaming) of variables for the next time step. After N_{ph} time steps and swapping, the variables at time levels $n - 1 + N_{ph}$ and $n + N_{ph}$, needed for the continuation of the next dynamical time step, will be updated by the same increment due to the physical parameterizations operating with a time step of $N_{ph}\Delta t$.

- 3) The input to the physics computations is the old saved model state valid at time level $n - 1$. Dynamical tendencies are needed for the turbulence- and convection parameterization. These tendencies are obtained as the difference between the model states $\gamma_{n-1+N_{ph}}$ and γ_{n-1} for variable γ . This difference represents an adiabatic model change which is the forcing to the physics during the long physics time step. The increment from the physical processes is supplied as a modification to the preliminary values available at time steps $n - 1 + N_{ph}$ and $n + N_{ph}$ used for the continued processing of a new time stepping cycle.

The methodology described above means that the physical parameterizations are forced with time averaged dynamical tendencies. This feature tends to produce a less ‘noisy’ interaction between the dynamics and the physics.

Optionally the turbulence parameterization can be computed with substepping in the physics. An appropriate dynamical increment may be added during the substeps. The argument for introducing such option is that turbulence is considered a process in balance with the dynamics on short time scales.

3. Physics

The role of physical parameterizations in an atmospheric model is to describe diabatic effects. In addition, the physics are necessary in order to obtain predictions of weather parameters such as rain and clouds. The physics comprise the processes of radiation and subgrid scale transports of momentum, temperature and moisture variables down to small scales associated with turbulence. In addition, the thermodynamics associated with latent heat release (e.g., condensation, evaporation, sublimation and precipitation) must also be described. The boundary conditions at the ground need also to be taken into account.

Parameterization of subgrid scale phenomena depends on the resolution of the model, because resolution defines an ability to resolve a given phenomenon. A simple example is the parameterization of cloud cover. In large scale models a stratiform cloud cover is often parameterized as a function of relative humidity, starting to become nonzero at a threshold relative humidity much below 100 percent, in order to account for subgrid scale variability of moisture. As the model resolution increases it is obviously not realistic to retain the cloud cover threshold at a fixed value, since the subgrid scale variability must decrease as the resolution becomes increasingly high.

It may therefore be concluded that physical parameterizations should depend on the resolution of the atmospheric model. As the model mesh size used in HIRLAM covers a range from that of a large scale model (around 50 km) to a size of about 5 km, it is to be expected that some adjustment of parameterizations with resolution is important. Two

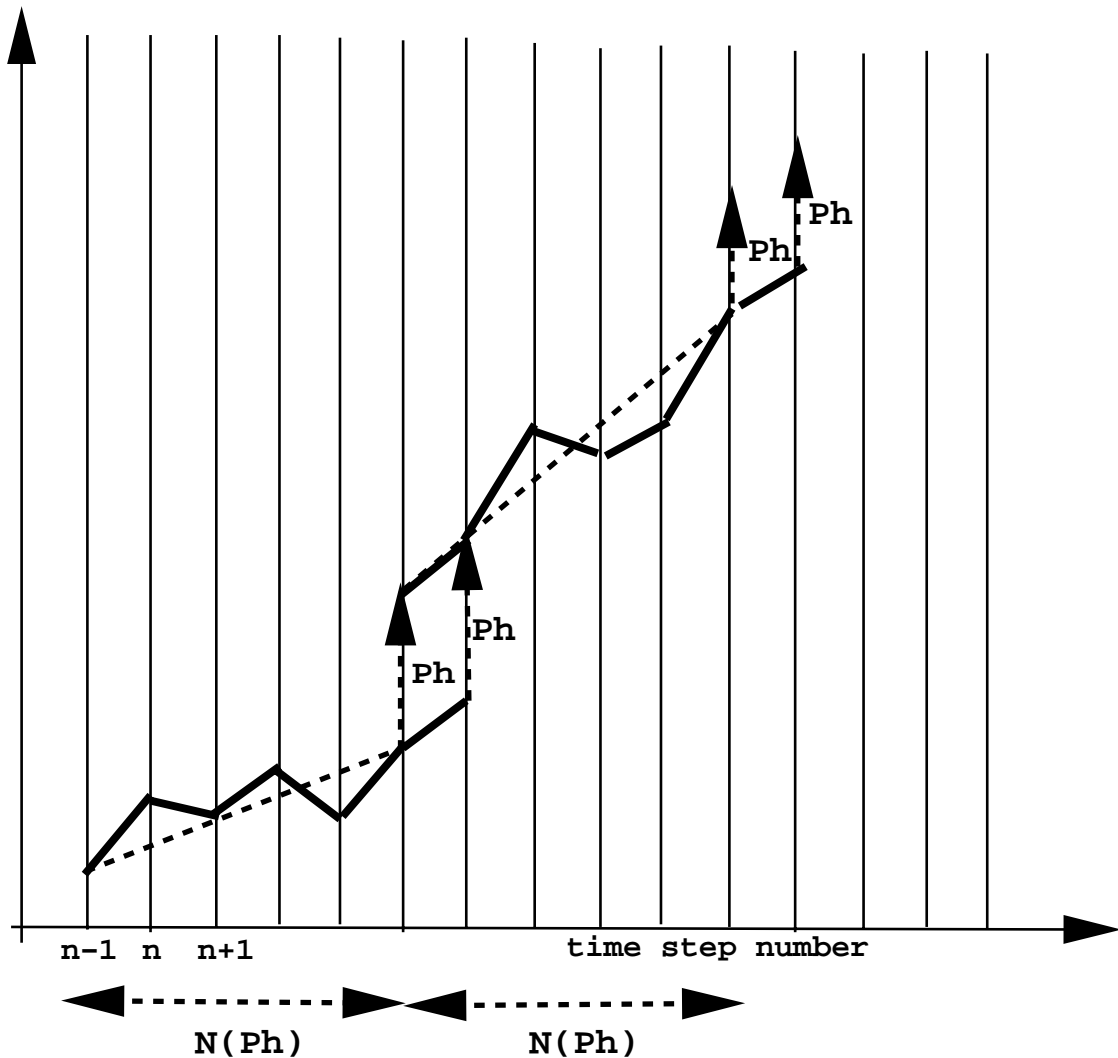


Figure 1: Time stepping cycle, vertical dashed arrows “Ph” represent the adding of physics increments valid for past N_{ph} time steps.

strategies are possible here. One may choose to do some tuning which is often rather ‘ad hoc’ for a modified resolution. This practice has been widely used in atmospheric modeling due to the lack of precise knowledge about a correct resolution dependence of physics.

Another approach is to realize that physics should be scale dependent and to formulate mathematical expressions for such dependencies, based on reasonable estimates for high and low resolutions. The latter approach has to some extent been applied in the formulation of condensation processes in the HIRLAM model (see subsection on clouds and condensation).

Each physical process has its own problems to address in high resolution. For radiation processes a challenging situation occurs at very high resolution since the transmission of radiation from neighboring grid boxes can contribute to the local heating rate. In

addition, the local cloud cover in a vertical column will in some situations not provide accurate information when computing solar radiation at the ground. This is because slant beams may pass through neighboring grid boxes with differing cloud amounts. Also the slope of the ground exposed to direct solar radiation becomes locally significant at high resolution, implying increased spatial variability of solar energy flux to the ground as resolution increases. These phenomena which become of some importance at resolutions below 10 km have not yet been addressed in the HIRLAM physics. The emphasis has been on describing radiative processes with reasonable accuracy in the troposphere. A fast radiation scheme (Savijärvi, 1990) has been further developed for HIRLAM (Sass et al., 1994). The scheme is normally called with the same frequency as other physical processes. This allows for describing radiation associated with fluctuating cloud cover at short time scales.

The atmospheric subgrid scale transports of heat, moisture and momentum at traditional model resolutions are dominated by the vertical transports. These take place over a large range of spatial scales, from large convective scales to small scales associated with turbulence. The goal is to describe accurately the effect of all subgrid scales on the resolved scales of motion. Traditionally these transports are separated into two scales, namely the small subgrid scales expressed by turbulence, and larger scales described by a convective parameterization. Due to the complexity of atmospheric states it is a challenge to make a coherent formulation of turbulence and convection parameterization.

In addition, the transports of moisture also has to describe phase changes. Therefore all processes connected to condensation and precipitation must be included. At increased model resolution more of the transports will be done by the resolved scale dynamics exposed to larger vertical velocities as a consequence of higher amplitude small scale convergence in the atmospheric flow. Hence the convection parameterization should accomplish less vertical moisture transports as the model resolution increases. A special problem associated with convection schemes is the break down at high resolution of the traditional assumption that convective cloud samples exist in balance with the synoptic forcing acting on the column of air above each grid square. There are indications (Emanuel, 1991) that convection needs to be parameterized at model resolutions below 10 km in order to take into account the very small scale convective updraft with high vertical velocities. However, the details on how to best incorporate a convection parameterization at a high model resolution (below 10 km) still appear to be an open question. The interaction of the model atmosphere with the ground takes place via complex processes of heat, moisture and momentum transfer. The surface processes are the boundary conditions for the vertical subgrid scale transports.

A special effect is created by subgrid scale orography exerting a gravity wave drag on the atmosphere. This effect which is considered important in synoptic scale models is currently not parameterized in HIRLAM. With increased model resolution this model limitation gradually diminishes. Currently the surface fluxes are described in terms of effective roughness lengths that may differ substantially for momentum, heat and moisture. The turbulent transports are communicated to the atmosphere by a diffusion scheme based on “turbulent kinetic energy” as a prognostic variable (Cuxart et al., 2000). The inclusion of this additional dependent model variable provides a better potential

to describe the effect of turbulent processes as compared to simple first order schemes. One reason is that the ‘memory’ of turbulence may be advected by the resolved flow. This represents an additional way for physics and dynamics to interact.

The extremely inhomogeneous and complex lower boundary condition with huge spatial variations of the physical properties of the surface in some regions makes it very difficult to parameterize accurately the averaged surface fluxes of momentum, heat and moisture. The first steps have been taken to improve the description of the lower boundary conditions supplied by physiographic data. New databases are utilized, e.g., a Global data base from the U.S. Geological Survey (USGS) and a local data base (Sattler, 1999).

The individual physical parameterizations of HIRLAM are described below.

3.1. Radiation

The purpose of the radiation parameterization scheme is to provide fluxes as a result of both solar radiation and infrared (thermal) radiation throughout the atmosphere. The temperature tendency providing the diabatic forcing to atmospheric motions may be written

$$\frac{\partial T}{\partial t} = -\frac{g}{c_p} \frac{\partial F_{net}}{\partial p}. \quad (20)$$

In (20) above T is temperature, t is time, g is the acceleration of gravity, c_p is the specific heat capacity of air at constant pressure, F_{net} is the integrated net radiation flux due to all significant wave lengths, and p is pressure.

The science behind radiation is in principle rather well understood. In practice, the computational demands required to carry out the so called ‘line-by-line’ calculations over the whole spectrum of interest are so extreme that such a strategy cannot be followed in a forecast model. Most forecast models perform radiative computations over rather few selected spectral intervals resolving the spectrum associated with solar radiation and thermal radiation.

The present radiation scheme treats radiation in a highly parameterized and simplified way. This allows for frequent calls to the radiation scheme such that, for example, the effect of changing cloud cover within short time scales can be accounted for. The fast radiation scheme (Savijärvi, 1990) developed for high resolution meso-scale models has been adopted. The scheme for parameterizing cloud effects has been developed further for HIRLAM purposes (Sass et al., 1994). The radiation scheme which is summarized below, does not attempt to explicitly resolve the radiation spectrum except for a separate treatment of ‘solar radiation’ and ‘thermal radiation’.

3.1.1. Shortwave radiation

The temperature tendency $\left(\frac{\partial T}{\partial t}\right)_s$ due to absorption of solar radiation is formulated according to

$$\left(\frac{\partial T}{\partial t}\right)_s = \left(\frac{\partial T}{\partial t}\right)_{sa} (1 - f_M) + \left(\frac{\partial T}{\partial t}\right)_{sc} f_M \quad (21)$$

The first term on the right hand side represents absorption in clear air, and the second term absorption in cloudy air. As an approximation we consider the cloudy fraction f_M to be equal to the maximum fractional cloud cover of all levels in a vertical column. In this formulation it is assumed that the maximum cloud cover applies to all levels below the uppermost cloud layer. Hence the cloud water content valid for clouds in a given model layer is scaled by a factor of $\frac{f}{f_M}$. A cloud water content $q'_c = \frac{q_c}{f_M}$ inside the cloud will then guarantee consistency between vertically integrated cloud water from the grid box model variable q_c and the vertically integrated cloud water used for the cloudy part of the shortwave computation. Above the uppermost cloud level the solar heating equals the clear air contribution.

It is necessary to specify at a given time the top of the atmosphere (TOA) solar flux S and the solar zenith angle θ . These are computed according to well known formulae from the literature (Paltridge and Platt, 1976). The heating rate of the clear air is computed according to (22–25), (Savijärvi, 1990)

$$\left(\frac{\partial T}{\partial t}\right)_{sa} = S \frac{q}{c_p} \frac{p}{p_0} [Y(u_s) + b_1 \alpha \cos \theta Y(u_*)] + b_2 (\cos \theta)^{0.3} \quad (22)$$

$$Y(u_s) = \begin{cases} b_3 u_s^{-0.81}, & u_s \geq 0.05 \text{ cm} \\ b_4 u_s^{-0.63}, & u_s < 0.05 \text{ cm} \end{cases} \quad (23)$$

$$u_s = \frac{1}{\cos \theta} u_{(0,p)} \quad (24)$$

$$u_* = \frac{1}{\cos \theta} u_{(0,p_s)} + b_1 u_{(p,p_s)}. \quad (25)$$

where

$$u_{(p_1,p_2)} = \frac{1}{g} \int_{p_1}^{p_2} q \frac{p}{p_0} dp$$

and α is the shortwave albedo of the ground. u_s is the slant direct beam, i.e., vertically integrated water vapour path linearly scaled by pressure and divided by $\cos \theta$ (in cm). u_* is the path length for isotropically reflected beams and $p_0 = 1013$ hPa is a reference pressure. The values of the constants b_1 to b_4 are given in Appendix C.

The two terms of (22) in brackets represent the absorption by water vapour in the direct and in the surface reflected beams, respectively. They are based on comparisons with line-by-line calculations (Chou, 1986). The last term in (22) is a parameterization of absorption by CO_2 , O_2 and O_3 , based on the standard absorption curves (Sasamori et al., 1972) and average amounts of these absorbing gases in the troposphere.

The cloud absorption is given by

$$\left(\frac{\partial T}{\partial t}\right)_{sc} = \hat{T}_{p_z,p} \left(\frac{\partial T}{\partial t}\right)_{sa} + \frac{g}{c_p} F_{sz} \frac{\partial}{\partial p} \hat{A}_{(p_z,p)}. \quad (26)$$

The total absorption is determined as the sum of the clear air absorption modified by the transmittance factor for the cloudy atmosphere (the first term) plus a major contribution from cloud drop absorption and increased path lengths due to scattering

(the second term). \hat{A} and \hat{T} are, respectively, the absorptance and transmittance from the top of the uppermost cloud layer to a level below. F_{sZ} is the solar flux density at the top of the uppermost cloud layer. This flux density is parameterized according to (27), as given originally for clear sky conditions at the ground, with $p = p_s$ (Savijärvi, 1990).

$$F_{sZ} = S \cos \theta \left[1 - 0.024 \cos \theta^{-0.5} - b_5 \cdot 0.11 \cdot u_s^{0.25} - b_6 \frac{p}{p_{00}} \left(\frac{0.28}{1 + 6.43 \cos \theta} - 0.07 \alpha_* \right) \right] \quad (27)$$

where $p_{00} = 1000$ hPa is a reference pressure. The first term in the brackets of (27) depending on the zenith angle θ concerns the stratospheric absorption due to ozone. A major contribution to the extinction of solar radiation comes from tropospheric absorption due to water vapour, CO₂ and O₂. This is parameterized according to the term involving u_s in (27). The last term involving two contributions describes the effect of scattering. The first contribution arises from scattering of the incoming solar beam while the second one is a compensating effect due to reflected radiation (from the cloud below having an albedo α_*), which is back-scattered from the atmosphere above. The coefficients, b_5 and b_6 , if larger than 1 (see Appendix C), represent a crude inclusion of effects due to aerosol absorption and scattering, respectively.

In order to define cloud layer absorptance and transmittance, simple formulae have been fitted to approximate results obtained with more detailed multiple scattering schemes (Slingo et al., 1982; Stephens, 1978; Liou and Wittman, 1979), for stratus type of droplet distributions.

$$\hat{A} = b_7 (b_8 + \cos \theta) \ln(1 + b_9 M_t) \quad (28)$$

$$\hat{T} = \frac{\hat{T}_1}{(\hat{T}_1 + M_t)}, \quad (29)$$

In (28) and (29) $\hat{T}_1 = b_{10}(b_{11} + \cos \theta)$ and M_t is the vertically integrated cloud water content (in g/m²) from the top of the uppermost cloud layer to a level below. Values of the constants b_7 to b_{11} are given in Appendix C. Finally, the net solar flux at the ground F_{s0} is computed according to (30) as a product of $(1 - \alpha)$ and a weighted sum of a clear air contribution F_{s0a} determined from a formula similar to (27), plus a cloudy contribution F_{s0c} according to (31):

$$F_{s0} = (1 - \alpha)[F_{s0a}(1 - f_M) + F_{s0c}f_M] \quad (30)$$

$$F_{s0c} = F_{sZ} \frac{\hat{T}_{(p_Z, p_s)}}{1 - \alpha(1 - \hat{T}_{(P_Z, P_s)})b_{12}} \quad (31)$$

The denominator in (31) takes into account multiple reflections between ground and cloud. The factor b_{12} accounts for absorption in reflected beams. This heating term, usually small, is included as a uniformly distributed heat source below the cloud top. Multiple reflections between two cloud layers are not explicitly included in the scheme.

3.1.2. Longwave radiation

The longwave scheme is based on an empirical emissivity function $e(p_{i-\frac{1}{2}}, p_{j+\frac{1}{2}})$ defined according to (32)

$$e(p_{i-\frac{1}{2}}, p_{j+\frac{1}{2}}) = a_1 + a_2 X - a_3 X^2 - a_4 X^3, \quad (32)$$

where

$$X = a_5 \ln \left(\sum_{k=i}^j q_k \frac{p_k}{p_{00}} \frac{\Delta p_k}{10g} \right)$$

The water vapour path has been scaled linearly with pressure. The values of the constants a_1 to a_5 are given in Appendix C. The clear air cooling rate based on (32) takes into account cooling due to water vapour line spectrum. It can be shown (Savijärvi, 1990) that the cooling rate may be written as a sum of three terms. One term expressing “local cooling to space” is usually significantly larger than are the other terms in the free atmosphere. A second term expressing interaction between the surface and the atmosphere is of significance close to the ground. A third term which determines the exchange of radiation with other layers is usually small and is neglected in clear sky calculations. Also a complete interaction between levels is avoided for the cloudy part of the computations. However, the significant effect of radiative interaction between clouds is retained as described in Appendix C. These simplifications may be defended only with reference to computational efficiency which is increased since the number of calculations become proportional to the number of model levels, and not to the number of levels squared.

Formally, the computation of the radiative temperature tendency due to thermal radiation is split up into four parts

$$\left(\frac{\partial T}{\partial t} \right)_i = \left(\frac{\partial T}{\partial t} \right)_{i1a} + \left(\frac{\partial T}{\partial t} \right)_{i2a} + \left(\frac{\partial T}{\partial t} \right)_{i1c} + \left(\frac{\partial T}{\partial t} \right)_{i2c} \quad (33)$$

Each of the terms in (33) is a weighted contribution to the total tendency. The scheme applies to a maximum cloud overlap assumption. The first term (I) is the heating rate contribution from the clear air part of the grid box with no clouds above while the second term (II) is the clear air contribution with clouds above. Similarly, the third term (III) is the cloudy contribution without clouds above and the fourth term (IV) a contribution with clouds above. The cloud covers used in the computations are effective cloud covers where the customary assumption is made that “grey” clouds may be introduced by reducing the grid box fractional cloud cover f with the cloud emissivity. The computational details are given in Appendix C.

The downward surface flux from the clear atmosphere is obtained from (34). In addition to the summation of the contributions from all levels expressed by the Planck function $B(T_k)$ and the emissivity function (first term) three additional terms are added. The first one (a_9) corresponds to the flux contribution due to aerosols. The last two terms are added to describe the effect of water vapour continuum.

$$F_{i0a} = \sum_{k=1}^N B(T_k) \cdot [e(p_{k-\frac{1}{2}}, p_s) - e(p_{k+\frac{1}{2}}, p_s)] + a_9 + a_{10} \sqrt{q_N} + a_{11} q_N. \quad (34)$$

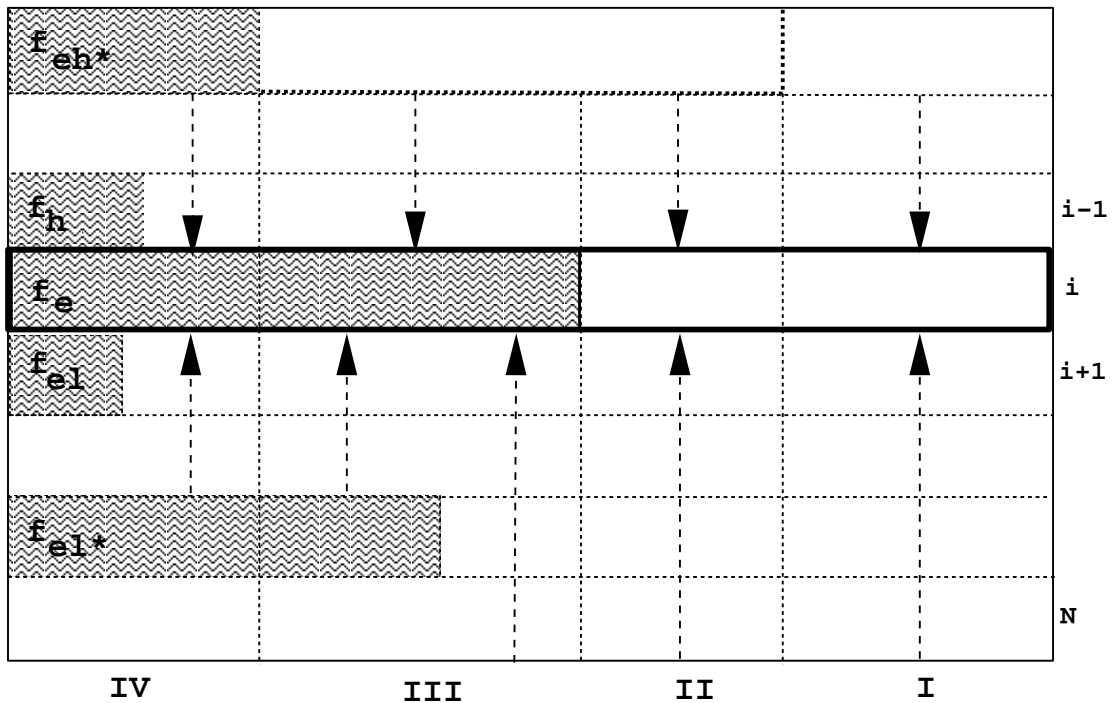


Figure 2: Computational scheme for infrared computations

Index N refers to the lowest model layer. The total downward flux from the atmosphere is obtained by adding a cloudy contribution F_{i0c} determined as radiation transmitted to the ground from an effective cloud cover according to the empirical expression in (35). The term in the square brackets is a fractional transmission estimated from the clear air contribution F_{i0a} and a low troposphere effective temperature T_{ef}

$$F_{i0c} = B(T_{h*})f_{eh*}(N) \left[1 - \frac{F_{i0a}}{(\sigma T_{ef}^4)} \right] \quad (35)$$

$$T_{ef} = T_N - a_{15} \left(\frac{\partial T}{\partial p} \right)_N \quad (36)$$

The net radiation at the ground due to longwave radiation follows from (37)

$$F_{i0} = \varepsilon_0 (F_{i0a} + F_{i0c} - \sigma T_{e0}^4) \quad (37)$$

σ is the Stefan Boltzmann's constant and ε_0 is the emissivity of the surface taken to be 0.95.

3.2. Turbulence

Turbulent transport of moisture, sensible heat and momentum plays an important role in the atmosphere. The parameterization of turbulence in numerical models of the

atmosphere is therefore of great concern. In recent years various turbulence schemes have been tested in HIRLAM. One such is a variant of the Louis scheme (Louis et al., 1982). In this scheme the vertical transports are based on local gradients of the forecast variables. A refined description of the unstable planetary boundary layer became available with a nonlocal first order scheme (Holtslag and Boville, 1993; Nielsen, 1998). Recently the potential of the turbulence parameterization has increased by introducing ‘turbulent kinetic energy’ as a prognostic variable. This scheme (Cuxart et al., 2000) is briefly described below.

3.2.1. Equations

The effect of turbulence on the mean flow is approximated by

$$\frac{\partial \bar{u}}{\partial t} = -\frac{\partial \overline{u'w'}}{\partial z}, \quad (38)$$

$$\frac{\partial \bar{v}}{\partial t} = -\frac{\partial \overline{v'w'}}{\partial z}, \quad (39)$$

$$\frac{\partial \bar{\theta}}{\partial t} = -\frac{\partial \overline{\theta'w'}}{\partial z}, \quad (40)$$

$$\frac{\partial \bar{q}}{\partial t} = -\frac{\partial \overline{q'w'}}{\partial z}, \quad (41)$$

$$\frac{\partial \bar{q}_c}{\partial t} = -\frac{\partial \overline{q'_c w'}}{\partial z}, \quad (42)$$

i.e. the horizontal derivatives of the second order covariance (Reynolds) terms are assumed to be much smaller than the vertical derivatives. θ is potential temperature in (40). Note that specific cloud water (q_c) is included as a prognostic variable. To the same level of approximation the equation for turbulent kinetic energy takes the form

$$\begin{aligned} \frac{\partial \bar{E}}{\partial t} = & - \left[\overline{u'w'} \frac{\partial \bar{u}}{\partial z} + \overline{v'w'} \frac{\partial \bar{v}}{\partial z} + \overline{w'w'} \frac{\partial \bar{w}}{\partial z} \right] \\ & + \left[\frac{g}{\theta_v} \overline{w'\theta'_v} \right] - \left[\frac{1}{\rho} \frac{\partial \overline{p'w'}}{\partial z} \right] - \left[\frac{\partial \overline{E'w'}}{\partial z} \right] - \varepsilon \end{aligned} \quad (43)$$

In (43) $\bar{E} = \frac{1}{2} \overline{(u'^2 + v'^2 + w'^2)}$ is the turbulent kinetic energy and ε is the dissipation of \bar{E} . Other symbols have their usual meaning. All terms on the r.h.s. represent the effect of physics. The first two terms are the horizontal shear productions of turbulent kinetic energy. The third term involving vertical velocity variance has currently been neglected. Also the fifth term involving pressure correlations has been neglected.

The fourth term involves buoyancy generated turbulence and the sixth term describes the vertical convergence of subgrid scale vertical transports of \bar{E} . Finally the last term is the dissipation term for \bar{E} .

The parameterization relates the second order moments to mean variables by assuming relations of the form

$$-\overline{\zeta'w'} = K_\zeta \left(\frac{\partial \bar{\zeta}}{\partial z} \right); \quad \zeta = u, v, \theta, q, q_c, E. \quad (44)$$

In (44) K_ζ is an eddy exchange coefficient analogous to the molecular viscosity and diffusivity coefficients. The eddy exchange coefficients depend on \overline{E} :

$$K_\zeta = c_\zeta K_u \phi_3 (Rs), \quad (45)$$

where c_ζ is a non-dimensional constant and $K_u = l\sqrt{\overline{E}}$ is the eddy exchange coefficient for momentum. ϕ_3 is a function of the dry Redelsperger number Rs

$$Rs = \frac{g}{\theta_v} \frac{l^2}{\overline{E}} \left(1 + 0.61 \overline{q} \frac{\partial \overline{\theta}}{\partial z} + 0.61 \overline{\theta} \frac{\partial \overline{q}}{\partial z} \right). \quad (46)$$

ϕ_3 takes the form (Cuxart et al., 1995)

$$\phi_3 = (1 + 0.139 \cdot Rs)^{-1}, \quad (47)$$

where Rs is controlled by the condition $Rs = \max\{-3.924, \min\{Rs, 71935.252\}\}$. The scheme is prepared for a change from the “dry” variables θ, q and q_c to the “moist” variables θ_l (liquid water potential temperature) and $q_{tot} = q + q_c$ (total specific humidity). The Redelsperger number should for example be replaced by its moist version, i.e. the vertical gradients of $\overline{\theta}$ and \overline{q} in (46) should be replaced by corresponding gradients of $\overline{\theta}_l$ and \overline{q}_t . Note that the covariance $\overline{E'w'}$ is retained in the TKE equation (43). Accordingly, the list of variables in (44) is expanded with $\zeta = E$.

The dissipation ε is treated in by the following expression

$$\varepsilon = c_\varepsilon \cdot \frac{\overline{E}^{3/2}}{l}, \quad (48)$$

In the equation above l is a diagnostic mixing length. It is computed from

$$l = \sqrt{l_u \cdot l_d}, \quad (49)$$

where l_u and l_d are the distances an air parcel must be displaced upward or downward, respectively, before its \overline{E} has been consumed by buoyancy. Currently a diagnostic lower boundary condition is specified for \overline{E} at the bottom level (index N). It is specified as

$$\overline{E}_N = 3.75u_*^2 + \delta_u \left[u_*^2 \left(-\frac{z_N}{L} \right)^{2/3} + 0.2w_*^2 \right], \quad (50)$$

with $\delta_u = 1$ or 0 if the surface layer is unstably or stably stratified, respectively. In the equation above L is the Monin-Obukov length scale (Businger et al., 1971). w_* is the convective velocity scale (Deardorff, 1972) and u_* is the friction velocity.

3.2.2. Numerical aspects

A semi-implicit treatment of the dissipation term of (43) has been made by writing (43) in the form

$$\frac{\partial \overline{E}}{\partial t} = F(\overline{E}, p_j), \quad j = 1, \dots, J \quad (51)$$

In (51) p_j , $j \leq J$ are parameters other than \bar{E} . The virtues of time schemes involving the partial derivative with respect to the prognostic parameter considered, in this case \bar{E} , have been discussed in the literature, e.g., (Kalnay and Kanamitsu, 1988) and (McDonald, 1998). The solutions are normally stable and free of spurious oscillations (noise). This idea can in principle be implemented for all terms on the r.h.s. of (43). The scheme reads (evaluating F at the middle of the time step)

$$\frac{(\bar{E}_{n+1} - \bar{E}_n)}{\Delta t} = F_n + \frac{1}{2} \left(\frac{\partial F}{\partial \bar{E}} \right)_n (\bar{E}_{n+1} - \bar{E}_n) \quad (52)$$

Currently the idea expressed by (51) and (52) has been implemented for the dissipation term only (Sass, 1999).

The finite difference approximation to (52) and (51) is incorporated to the set of finite difference equations representing (43). The finite difference equation at model level k may be written

$$\begin{aligned} \bar{E}_{k,n+1} = & \bar{E}_{k,n} + S_k + S_k^\epsilon + S_k^{\epsilon*} + A_{k,n}(\bar{E}_{k-1,n+1} - \bar{E}_{k,n+1}) \\ & - C_{k,n}(\bar{E}_{k,n+1} - \bar{E}_{k+1,n+1}) - D_k^* \bar{E}_{k,n+1} \end{aligned} \quad (53)$$

In (53) S_k is a source term as a result of sheer production and buoyancy production of \bar{E} . The term S_k^ϵ is an explicit dissipation term in agreement with (48). The terms $S_k^{\epsilon*}$ and D_k^* including '*' are additional terms connected to the implicit treatment utilizing (51) and (52). $S_k^{\epsilon*} = \frac{3}{4} \frac{c_\epsilon}{L} \bar{E}_n^{\frac{3}{2}} \Delta t$ and $D_k^* = \frac{3}{4} \frac{c_\epsilon}{L} \bar{E}_n^{\frac{1}{2}} \Delta t$.

When these terms are neglected, (53) reduces to the system using explicit dissipation. The coefficients $A_{k,n}$ and $C_{k,n}$ are coefficients involving eddy exchange coefficients describing turbulence effects from above and below level k , respectively.

From (53) one may isolate $\bar{E}_{k,n+1}$ on the left hand side giving

$$\bar{E}_{k,n+1} = \frac{\bar{E}_{k,n} + S_k + S_k^\epsilon + S_k^{\epsilon*} + A_{k,n} \bar{E}_{k-1,n+1} + C_{k,n} \bar{E}_{k+1,n+1}}{1 + A_{k,n} + C_{k,n} + D_k^*} \quad (54)$$

(54) describes a coupled set of equations in $\bar{E}_{k,n+1}$, $k = 2, \dots, M-1$. M is the number of model layers. At the top ($k=1$) an equation applies with $A_{1,n} = 0$. Similarly, for the bottom layer $C_{M,n} = 0$. The system of equations is solved by standard methods (successive elimination and backward substitution).

3.3. Convection and condensation

There has been many approaches during the past decades to describe the processes connected to clouds and condensation. This is related to the fact that a description of cloud and condensation processes involves both micro-physical aspects and a formulation of the vertical subgrid scale transports on all scales (turbulence and convection). Furthermore, it is often difficult to validate which formulations should be preferred by means of solid observational evidence. In recent years international comparisons have been useful

as a guidance, e.g., the GEWEX (Global Energy and Water Cycle Experiment) cloud system study (GCSS).

In the HIRLAM community a review on the use of convection schemes in mesoscale models has been written recently (Bister, 1998). One trend has been to apply mass flux concepts to parameterize convection. It may be argued that a mass flux approach is more physically based than are formulations relying on alternative approaches.

The different ideas and hypotheses behind parameterizing convection are reflected in the availability of different convection schemes for experimentation in the HIRLAM forecasting system. All schemes used in HIRLAM have ‘cloud condensate’ available as a prognostic variable which is advected by the model dynamics.

Currently the operational convection scheme is based on a moisture convergence closure and may be viewed as a further development of the ideas expressed by Kuo (1974). The scheme named STRACO stands for ‘Soft TRAnSition CONdensation’ and concerns gradual transitions between convective and stratiform regimes.

The moisture convergence closure includes the effect of surface evaporation flux. A formulation of the vertical redistribution of cloud condensate is included which is an extension of the original formulations. Also convection can start from any level in the atmosphere whereas several convection schemes treat only deep convection originating from the lowest model layer.

The vertical extent of convection is determined by adiabatic cloud parcel lifting including latent heat release, starting with a small temperature excess as a ‘trigger’ for convection. Entrainment and detrainment are not explicitly taken into account during parcel lifting, but a simple constraint inhibits the vertical extent of convective clouds in case of a weak net convergence of moisture. Otherwise the level of non-buoyancy determines the top of the convective layers forming a convective entity. Formally there is no limit on the possible number of convective entities in the vertical air column. The relevant equations are :

$$\left(\frac{\partial q}{\partial t}\right)_{ADC} = \left(\frac{\partial q}{\partial t}\right)_{AD} (1 - \delta_*) + \widehat{Q}_a \beta \frac{F_q}{\widehat{F}_q} \delta_* + K_c q_c (q_s - q_e) + E_{pc} \quad (55)$$

$$\left(\frac{\partial q_c}{\partial t}\right)_{ADC} = \left(\frac{\partial q_c}{\partial t}\right)_{AD} + \widehat{Q}_a (1 - \beta) \frac{F_c}{\widehat{F}_c} \delta_* - K_c q_c (q_s - q_e) - G_{pc} \quad (56)$$

$$\left(\frac{\partial T}{\partial t}\right)_{ADC} = \left(\frac{\partial T}{\partial t}\right)_{AD} + \frac{L'}{c_p} \left(\widehat{Q}_a (1 - \beta) \frac{F_h}{\widehat{F}_h} \delta_* - K_c q_c (q_s - q_e) \right) - \frac{L'}{c_p} E_{pc} \quad (57)$$

The left hand sides of these equations express the combined effect of both dynamical advection, turbulence and convection. $\frac{\partial}{\partial t}()_{AD}$ signifies a tendency excluding convection. \widehat{Q}_a is the total moisture accession per unit mass and time in the convective cloud. L' and c_p represent the specific latent heat of fusion or sublimation, depending on the micro-physical conditions, and the specific heat capacity at constant pressure, respectively.

F_h is a function describing the vertical variation of convective heating.

$$F_h = T_{vc} - T_{ve} + \epsilon_T \quad (58)$$

F_q is a function describing the vertical variation of convective moistening.

$$F_q = q_{sc} - q_e + \epsilon_q \quad (59)$$

F_c is a function describing the vertical variation of convective condensate supply.

$$F_c = q_{cc} + \epsilon_c \quad (60)$$

In the above equations for F_h , F_q and F_c index v stands for ‘virtual’. Index e means ‘environmental’ (outside clouds). \widehat{F} stands for a vertical average value for the convective cloud. Finally, c -index means a value applicable to cloud and s signifies a saturation value. The constants $\epsilon_T, \epsilon_q, \epsilon_c$ are currently set to zero.

The parameter β is a moistening parameter (Kuo, 1974). In the present scheme, contrary to models without prognostic cloud condensate, moistening can take place also from evaporation of cloud condensate.

$$\beta = \left(1 - \frac{\sum_{j=jbot}^{jtop} \frac{q}{q_s} \Delta p}{p_{jbot} - p_{jtop}} \right)^{\gamma_0} \quad (61)$$

Here p represents ‘pressure’, and $jbot$ and $jtop$ are the model level numbers for the bottom and top of convection, respectively. Currently γ_0 is set to a value of 2. The parameter δ_* is an important one, because it determines a link between convective moisture transports on one hand and turbulence plus dynamics effects on the other.

$$\delta_* = B \left(\frac{\Delta p_c}{p_{00}} \right)^{\gamma_1} \left(\frac{\Delta \theta}{\theta_{00}} \right)^{\gamma_2} \quad (62)$$

A resolution dependence has been introduced through the scaled latitude increment $\Delta \theta$ for the given resolution. The term involving Δp_c and p_{00} is a scaled cloud depth. Currently $\theta_{00} = 0.15^\circ$ and $p_{00} = 10^4$ Pa. γ_1 and γ_2 are equal to 1. Both factors are constrained to be no larger than 1. The effect of this formulation is that δ_* goes to zero for extremely shallow phenomena and for very high horizontal resolution. A zero δ_* means that the convection scheme is decoupled as is reasonable in the limit of very shallow phenomena and high resolution where dynamics and turbulence should suffice. The factor B is a dimensionless buoyancy which is zero for a vanishing mean buoyancy in the convective cloud but becomes 1 when cloud buoyancy exceeds a small threshold. It serves to prevent an abrupt switch from stratiform to convective regime.

The third term in the main equations involving $(q_s - q_e)$ is an evaporation/sublimation term of cloud condensate. (K_c is a constant). A similar formulation, involving cloud cover as the leading term in place of q_c , has been used by others, e.g., (Tiedtke, 1993) in the ECMWF cloud scheme.

Finally, the terms involving G_{pc} and E_{pc} concern generation and evaporation of convective precipitation, respectively.

The equations above are applied in the layers of the convective entities while the stratiform condensation apply to the remaining parts of the atmosphere.

Associated with each convective and stratiform layer, respectively, is an equilibrium statistical distribution of total specific humidity around a grid box average value \bar{q}_{tot} .

In the stratiform case a symmetric rectangular density function is assumed and super-saturation is defined with respect to the grid box saturation specific humidity $q_s(\bar{T})$. In the convective case an asymmetric density function is assumed and super-saturation is defined with respect to a saturation humidity corresponding to a characteristic air parcel temperature T_c associated with convection. These assumptions make it feasible to define the fraction of the grid square which is saturated. This is by definition the grid box cloud cover.

The cloud fractions f_{cv} and f_{st} for convective and stratiform clouds respectively are given below

$$f_{cv} = \frac{1}{1 + \sqrt{\frac{q_s(T_c) - \bar{q}}{\bar{q}_c}}} \quad (63)$$

In (63) $q_s(T_c) \geq \bar{q}_{tot}$. An intermediate range is defined if $\bar{q}_{tot} \cdot (1 - A_{cv}) \leq q_s(T_c)$ and $q_s(T_c) < \bar{q}_{tot}$, where A_{cv} is a dimensionless threshold ~ 0.1 defining the width of the lower part of the probability density function of q_{tot} . For this intermediate range

$$f_{cv} = \frac{1}{2} + \frac{(\bar{q}_{tot} - q_s(T_c))}{2A_{cv}\bar{q}_{tot}} \quad (64)$$

Finally, f_{cv} is constrained to be equal to 1, if $q_s(T_c) < \bar{q}_{tot}(1 - A_{cv})$.

Correspondingly the following equation applies to the stratiform cloud cover f_{st}

$$f_{st} = \frac{1 + A_{st} - \frac{q_s(\bar{T})}{\bar{q}_{tot}}}{2A_{st}} \quad (65)$$

The formula above is only used in the range where it provides a cloud cover between zero and one. Outside this range the cloud cover is either 0 or 1, respectively. The probability function for q_{tot} also defines the equilibrium cloud condensate. It is assumed that also the specific humidity at sub-saturation is distributed equally as a rectangular probability function around the grid box average value \bar{q} . The amplitude of the fluctuating q_{tot} , as defined by A_{st} is constrained not to violate a rectangular distribution of q .

A similar approach for describing subgrid scale condensation has been used others in the literature (Redelsperger and Sommeria, 1986). They emphasize the virtues of having a subgrid scale parameterization of condensation even at horizontal resolutions of a few kilometers grid distance.

The amplitude A_{st} of the symmetric density function for total specific humidity in the stratiform case should ideally not be constant with model resolution. The estimates (Redelsperger and Sommeria, 1986) that the subgrid scale effects should go to zero quite slowly at high resolution combined with typical values used in coarse resolution models have been used as a guidance for constructing (66) below. This effect of resolution is described by the first factor in (66). Formulations of A_{st} depending on other factors such as the height above ground have been suggested (Sundqvist et al., 1989). He assumes a

decrease of A_{st} of the subgrid scale variability close to the ground. A similar idea has been adopted in the STRACO scheme as expressed by the term in the second brackets of (66).

$$A_{st} = A_{st1} \left(1 - \exp(-A_{st2} \sqrt{D_{gr}}) \right) \left(\frac{A_{st3} + A_{st4}(1 - \sigma_{st}^3)}{A_{st3} + A_{st4}} \right) \quad (66)$$

In (66) $A_{st1} = 0.30$, $A_{st2} = 0.003$, $A_{st3} = 0.03$, $A_{st4} = 0.02$. $\sigma_{st} = \min(\frac{p}{p_{st}}, 1)$. $P_{st} = 1013$ hPa. D_{gr} is the distance in metre between neighboring grid points.

A relaxation towards the equilibrium is applied to define stratiform condensation. However, the constraint is always imposed that gridbox saturation is not exceeded. Condensation associated with equilibrium is determined by a first order adjustment.

$$\Delta q_{st} = \frac{(q_c - q_{ceq})}{1 + f_{st} \frac{L}{c_p} \left(\frac{\partial q_s}{\partial t} \right)} \quad (67)$$

Due to the changing conditions as regards q , q_c and T in a model layer, the ‘equilibrium’ distribution is disturbed. This may, for example, happen with the onset of stratiform conditions after convection or vice-versa. To describe the actual transitions the cloud cover f is made time dependent by relaxing towards the equilibrium cloud cover f_{eq} which may be either a stratiform (f_{st}) or a convective equilibrium (f_{cv}).

$$\frac{\partial f}{\partial t} = -K_f (f - f_{eq}) \quad (68)$$

Currently $K_f^{-1} = 900$ s.

The micro-physics related to the condensation and precipitation processes follow rather closely the comprehensive treatment by (Sundqvist, 1993).

4. Surface treatment

4.1. Fluxes of momentum, heat and moisture at the surface

Turbulent surface fluxes in numerical weather prediction models are traditionally computed from drag formulae relating the surface fluxes to the mean states of the surface and of the atmosphere at the observation height (in a numerical model, typically the lowest model level). The drag coefficient C_γ for a scalar variable γ is defined by the equation

$$\overline{w'\gamma'} = C_\gamma \Delta\gamma |\vec{V}_N| \quad (69)$$

in which $\overline{w'\gamma'}$ is the vertical turbulent kinematic flux of γ and $\Delta\gamma = \gamma_s - \gamma_N$.

The scalar variables and the wind vector on the right hand side of (69) are time averages like the flux term on the left hand side, but for convenience the averaging symbol has been omitted on the right hand side. The sign convention in (69) is such that upward fluxes are positive.

Over the ocean \vec{V}_N should, strictly speaking, be measured in a frame moving with the ocean surface current and T_s should be the surface skin temperature.

The surface specific humidity q_s is not so obvious to specify as compared to surface wind speed \vec{V}_s which may be assumed to be zero.

Over sea the saturation value $q_{sat}(T_s)$ with respect to the surface temperature is assumed. Over land a soil wetness parameter $F_{wet} = a_{w1} + (1 - a_{w1})(\frac{W_s}{W_{sat}})^{a_{w2}}$. W_s and W_{sat} are defined in the next subsection. $a_{w1} = 0.05$. $a_{w2} = 8$. The constraint is always imposed that the saturation value $q_{sat}(T_s)$ is never to be exceeded.

$$q_s = F_{wet}q_{sat}(T_s) + (1 - F_{wet})q_N \quad (70)$$

In the current formulation

$$C_\gamma = C_{MN} \left(1 + \ln \frac{z_{0M}}{z_{0H}} / \ln \frac{z}{z_{0M}} \right)^{-1} \Psi_\gamma \left(Ri, \frac{z}{z_{0H}}, \frac{z}{z_{0M}} \right) \quad (71)$$

This formulation is used for different surface types and forecast scalar parameters. ($\gamma = M$ for momentum, correspondingly H and Q stand for heat and moisture transfer, respectively). The two factors in front of the function Ψ_γ form a neutral drag coefficient $C_{\gamma N}$. For identical roughness lengths z_{0M} and $z_{0\gamma}$ the second factor in the brackets becomes unity and $C_{\gamma N} = C_{MN}$.

$$C_{MN} = \left(\frac{k}{\ln(\frac{z}{z_{0M}})} \right)^2$$

$k \sim 0.4$ is the von Kármán constant.

The functions used for Ψ_γ follow the work of (Louis, 1979) and (Louis et al., 1982).

The following form applies to the unstable atmospheric boundary layer:

$$\Psi_\gamma = 1 + \frac{a_{\gamma U} Ri}{1 + b_{\gamma U} C_{\gamma N} (Ri \frac{z}{z_{0M}})^{\frac{1}{2}}} \quad (72)$$

In (72) above Ri is the surface bulk Richardson number. $a_{mU} = 10$, $b_{mU} = 75$, $a_{HU} = a_{QU} = 15$ and $b_{HU} = b_{QU} = 75$

A special situation occurs as the mean horizontal wind speed goes to zero in an unstable boundary layer. It turns out that realistic surface fluxes can be achieved in the framework of the existing formula provided that z_{0M} in (72) is replaced by the length scale d_γ , (Nielsen, 1999), where $d_M = 1.03 \frac{\nu}{u_{fc}}$, $d_H = d_Q = 1.14 \frac{\nu}{u_{fc}}$, and ν is a kinematic viscosity of air. u_{fc} is a velocity scale associated with free convection

$$u_{fc} = \left(\frac{g}{\theta_v} \Delta\theta_v \nu \right)^{\frac{1}{3}} \quad (73)$$

In (73) g is the acceleration of gravity and $\Delta\theta_v$ expresses the virtual potential temperature difference between the atmosphere and the sea surface.

For the stable boundary layer the corresponding formula is

$$\Psi_M = \frac{1}{1 + \frac{a_{MS} Ri}{\sqrt{1 + b_{MS} Ri}}} \quad (74)$$

In (74) above $a_{MS} = 10$, $b_{MS} = 1$.

For heat and moisture the following function is used

$$\Psi_\gamma = \frac{1}{1 + a_{\gamma S} Ri \sqrt{1 + b_{\gamma S} Ri}} \quad (75)$$

$a_{HS} = a_{QS} = 10$ and $b_{HS} = b_{QS} = 1$.

For flux computations over land and sea ice the potential of the formulae above to incorporate effects of separate roughness lengths for momentum, heat and moisture, is not used. Currently the roughness lengths for heat, moisture and momentum are taken to be equal. The actual value of roughness depends strongly on land surface type according to basic theories of the planetary boundary layer (Garrat, 1977). The actual values are computed in the climate field generation (see subsection 4.3). Values of heat and moisture roughness up to 0.5 m are allowed for. However, it turns out that larger values for momentum roughness are needed to describe surface drag in a formulation based on roughness length. This is because the effect of subgrid scale orography is significant. The current algorithm for such computations makes the momentum roughness proportional to the variance of subgrid scale orography. In this way it turns out that momentum roughness over land can achieve values of several metre. The roughness length for ice is taken to be 0.03 m which is substantially higher than current estimates for a plane ice surface, in order to account for horizontal irregular features occurring in natural ice fields.

To complete the parameterization for surface flux computations over sea the ratio of the roughness lengths z_{0M}/z_{0H} and z_{0M}/z_{0Q} must be related to known quantities. Measurements over sea indicate that the surface roughness lengths for momentum, sensible heat and moisture are different, (DeCosmo et al., 1996). The main reason is probably that form drag (i.e., momentum transport by pressure forces) in the presence of sea waves enhances the momentum transfer, while the heat and moisture transfers at the air-sea interface are controlled by molecular diffusion alone.

According to observations and laboratory experiments z_{0M} depends on the sea state. At low wind speeds laboratory experiments indicate that the sea surface becomes aerodynamically smooth with $z_{0M} = 0.11 \nu / u_*$. At sufficiently high wind speeds the sea surface becomes aerodynamically rough. In the latter conditions the Charnock formula $z_{0M} = \beta u_*^2 / g$, (Charnock, 1955) with a value of β in the range of 0.011 to 0.032, are widely used. In numerical models values of β in the interval of 0.014 to 0.0185 are recommended (Garrat, 1992). We introduce a transition in z_{0M} from a smooth to a rough sea surface depending on wind speed $|\vec{V}_N|$, where index N refers to the height of the lowest model level. The interpolation formula for z_{0M} is specified as

$$z_{0M} = (1 - \xi(\mathbf{u})) 0.11 \nu / u_* + \xi(\mathbf{u}) \beta \frac{u_*^2}{g}, \quad (76)$$

with

$$\xi(\mathbf{u}) = \left[\max \left(\min \left(\frac{u - u_s}{u_r - u_s}, 1 \right), 0 \right) \right]^{1/2}. \quad (77)$$

In (76) and (77) $u = |\vec{V}_N|$, $u_s = 3.0$ m/s and $u_r = 5.0$ m/s. According to (76) and (77) the sea surface is considered to be smooth for $u \leq 3$ m/s and rough for $u \geq 5$ m/s. The transition interval is somewhat smaller than the interval from 2.5 to 5.5 m/s usually found in the literature e.g., (Garrat, 1992). Over open sea (here defined as fraction of sea equal to 1) β has been set to 0.014, otherwise $\beta = 0.032$. The former value fits measurements over the open ocean quite well, e.g., (Yelland and Taylor, 1996; Grachev et al., 1998). A higher value of β (larger momentum flux) in shallow coastal waters is supported by measurements (Oost, 1998; Hansen and Larsen, 1997; Maat et al., 1991), although the governing parameter for z_{0M} seems to be the wave age.

We assume that z_{0H} and z_{0Q} can be related to z_{0M} . Observational evidence of a relation between z_{0M} and z_{0Q} has been presented for example by DeCosmo *et al.*, 1996. Dependence of z_{0H} and z_{0Q} on z_{0M} are also key features in ‘surface flux over sea’ models by e.g. (Clayson et al., 1996; Liu et al., 1979; Brutsaert, 1975). In our parameterization z_{0H} and z_{0Q} are related to z_{0M} by formulae suggested in Garratt, 1992. In terms of the roughness Reynolds number Re_* the relations take the form

$$\ln \frac{z_{0M}}{z_{0H}} = \alpha_H Re_*^{1/4} - 2, \quad (78)$$

$$\ln \frac{z_{0M}}{z_{0Q}} = \ln \frac{z_{0M}}{z_{0H}} - \alpha_Q Re_*^{1/4}, \quad (79)$$

in which Re_* is defined as

$$Re_* = \frac{z_{0M} u_*}{\nu}, \quad (80)$$

i.e., by the sea surface momentum roughness length (z_{0M}), the surface friction velocity (u_*) and the molecular kinematic viscosity coefficient for air ($\nu \simeq 1.5 \cdot 10^{-5}$ m²/s). Over a rough sea $\alpha_H=2.48$ and $\alpha_Q=0.2$. With the transition from a smooth to a rough sea surface given by (77), and over a smooth surface with the requirement $z_{0\gamma} \cdot u_* / \nu = S_\gamma$ for $\gamma = H, Q$ and $S_H \approx 0.2$ and $S_Q \approx 0.3$ (Garrat, 1992), the coefficients α_H and α_Q in (78) and (79) become

$$\alpha_H = 0.05\xi(u) + 2.43, \quad (81)$$

$$\alpha_Q = -0.50\xi(u) + 0.70. \quad (82)$$

4.2. Surface energy and moisture budget

In the previous section the relevant interactions between atmosphere and surface were described, except as regards radiation fluxes which need also to be considered to describe the atmospheric forcing of the surface. The present treatment of the surface consists of separate computations for sea or lake surface on the one hand, and a land surface possibly including ice on the other. In the former case the interactions with the atmosphere happens via the fluxes of momentum, heat and moisture as described above, and as a result of radiation. In the infrared part of the spectrum the radiation is exchanged almost as black body radiation corresponding to the sea surface temperature (SST). The emissivity of the surface is currently taken to 0.95. The SSTs are achieved from the daily values received from ECMWF. An interpolation procedure takes into account

the distribution of sea and land. Any net energy loss from the sea surface has no direct consequences for the model SST because this parameter is not a prognostic variable, but is locally fixed in time during a forecast. The fraction of ice in a grid square is defined from the SST field assuming a linear increase of ice fraction between zero and one as the temperature changes from 0°C to -2°C .

The energy and moisture budget of a land surface needs to be treated in a prognostic sense since the forecasting of diurnal variations of meteorological parameters close to the ground is vital. The present surface treatment over land is simple. There are two prognostic surface temperatures, namely T_s and T_d respectively. T_s represents a surface temperature, and T_d a temperature at an intermediate level above a climatic deep soil temperature. Similarly, two prognostic equations are included for soil moisture (W_s and W_d). These variables represent soil moisture at the upper and at the intermediate level, respectively. Currently there is no assimilation scheme for soil parameters such as temperature and moisture. Instead the initial values used in a forecast come from a short range forecast.

4.2.1. Equations for soil variables

The evolution of temperature and soil water is assumed to obey a simple diffusion equation in a simple two layer soil model. Also an equation for snow depth S_n is available. The five prognostic equations are given below.

$$\frac{\partial T_s}{\partial t} = \frac{1}{\rho_s c_s D_1} \sum_i \Phi_i + \frac{\kappa_0(1 - k_{sn} F_{sn})(T_d - T_s)}{0.5 D_1 (D_1 + D_2)} \quad (83)$$

In the equation above $\sum_i \Phi_i = \Phi_R + \Phi_H + \Phi_Q$ are the surface net fluxes due to radiation, sensible heat and latent heat, respectively. $F_{sn} = \min(\frac{H_{sn}}{H_{snc}}, 1)$ is a snow fraction, with H_{sn} being snow depth and $H_{snc} = 0.015$ m a threshold snow depth in an equivalent height of water. T_s (K) is the soil temperature in the upper soil layer. T_d is the soil temperature in the intermediate soil layer. ρ_s is the soil density (kg/m^3), c_s is the specific heat capacity of the soil ($\frac{\text{J}}{\text{kg K}}$), κ_0 is the heat diffusivity of soil without snow cover (m^2/s). k_{sn} is a dimensionless constant used to reduce heat diffusivity if snow cover is positive.

Currently, $\rho_s c_s = 2.7 \cdot 10^6$ J/(m^3 K), $k_{sn} = \frac{2}{3}$, $D_1 = 0.07$ m, and $D_2 = 6D_1$.

$$\frac{\partial T_d}{\partial t} = -\frac{\kappa_0(T_d - T_s)}{0.5 D_2 (D_1 + D_2)} + \frac{\kappa_0(T_{cli} - T_d)}{D_2 D_3} \quad (84)$$

T_{cli} is a climatic deep soil temperature updated every month. $D_2 = D_3 = 6D_1$ (m).

Similarly, the equations for soil water are

$$\frac{\partial W_s}{\partial t} = (1 - F_{sn})\Phi_Q + P_{rn} + M_{sn} + \frac{\lambda(W_d - W_s)}{0.5 D_1 (D_1 + D_2)} \quad (85)$$

W_s is the soil water in the top layer (m). W_d is soil water in the second soil layer times $\frac{D_1}{D_2}$ (m). This means that it is scaled to the depth of the top layer. P_{rn} is the rain flux

density reaching the ground ($\frac{\text{kg}}{\text{m}^2\text{s}}$). M_{sn} is the change in snow depth per unit time. λ is a diffusivity for conduction of soil water. $\lambda = 1.0 \cdot 10^{-7} \text{ m}^2/\text{s}$.

$$\frac{\partial W_d}{\partial t} = -\frac{\lambda(W_d - W_s)}{0.5D_2(D_1 + D_2)} + \frac{\lambda(W_{cli} - W_d)}{D_2D_3} \quad (86)$$

Snow depth H_{sn} is updated if the the physiographic data-fields ‘fraction of land’ or ‘fraction of ice’ is positive in a model grid square.

$$\frac{\partial H_{sn}}{\partial t} = F_{sn} \frac{\Phi_Q}{\rho_{h2o}} + P_{sn} - M_{sn} \quad (87)$$

ρ_{h2o} is the density of water (kg/m^3).

The treatment of ‘runoff’ is very simple since instantaneous runoff of soil water is assumed if soil water exceeds 0.02 m (upper layer). This corresponds approximately to a volumetric water amount of 0.29.

Snow melt is crudely accounted for, being proportional to mean excess of land temperature over the melting point. The mean surface temperature, T_s , is allowed to rise above the melting point before all snow has melted, in order to account for subgrid scale temperature variation.

4.2.2. Numerical aspects

In order to prevent numerical instability, the equations above for the soil parameters γ are solved by the following semi-implicit method:

$$\frac{\partial \gamma}{\partial t} = \Psi(\gamma) \quad (88)$$

In the equation above Ψ is linearized in the following way: (n is the current time step, $n + 1$ is the new time step)

$$\Psi(n + 1) = \Psi(n) + \frac{1}{2} \frac{\partial \Psi}{\partial \gamma} (\gamma(n + 1) - \gamma(n)) \quad (89)$$

As a consequence of the equations above, the partial derivatives of surface fluxes with respect to the surface variable γ need to be computed.

4.3. Physiographic data

An accurate specification of the lower boundary conditions associated with atmospheric forecasts is very important, especially due to the need to forecast weather parameters close to the ground. Various surface fields (e.g., surface geopotential, surface albedo, surface roughness, soil temperature and soil moisture, and fractions of a grid square with sea (lake), ice and different types of land) are needed to carry out adequate surface computations. High quality and high resolution physiographic data are needed as a

basic source to compute the fields accurately. New databases and new software have been introduced recently for this generation of surface fields. The new software makes use of the *Hierarchical Data Format* HDF, which makes it possible to unify the format of the input files for the computation of the needed surface fields for HIRLAM.

The data bases are of different origin. One set used is the *Global 30 Arc Second Elevation data* (GTOPO30). A second one is the *Global Land Cover Characteristics data* (GLCC). These data sources have a horizontal resolution of about 1 km. Improved accuracy on the land use over Denmark has been obtained with local data from “Kort og Matrikelstyrelsen” in Copenhagen. The processing of data for generation of physiographic data for HIRLAM has been documented (Sattler, 1999).

5. Data assimilation

Application of a data assimilation system is necessary in order to analyse the initial state of a given forecast. Due to the limited number of observations in comparison to the number of model grid points the current practice is to correct a “first guess” from a recent forecast, with observations. In the HIRLAM analysis system this is done by the so called optimum interpolation method (Lorenç, 1981). A documentation of the HIRLAM analysis system is available (Källén, 1996; Lönnberg and Shaw, 1987).

Wind components, geopotential and surface pressure are analysed using a multivariate 3-dimensional statistical interpolation while a univariate interpolation is used for relative humidity. Analyses are made in a non-staggered grid. A comprehensive quality control, including a check against first guess values, is implemented to avoid the use of erroneous observations.

Analyses are made for standard pressure levels between 1000 hPa and 10 hPa.

Currently, the following observations are used: SYNOP (pressure only), SHIP (pressure, wind), DRIBU (pressure, wind), PILOT (wind), TEMP (geopotential, wind and humidity at standard levels), AIREP and AMDAR/ACARS (wind).

The analysis computations are carried out in the following sequence:

- 1) Extraction of observational data and moving platform redundancy check and data thinning (see (Undén, 1999) for the latest changes).
- 2) Interpolation of first guess fields and first guess error standard deviation fields to the observational positions. Bilinear interpolation is used in the horizontal and tension spline is used in the vertical.
- 3) Formation of superobservations by averaging observed values of the same data types over areas corresponding to the analysis grid resolution. Superobservation formation is preceded by a quality control to avoid superobservation values to be influenced by erroneous data.

- 4) Analysis check and final rejection/acceptance of observed data for the grid point analysis. This is done by inversion of the large covariance matrices for each analysis box, reduction of the inverted matrices to suppress influence of the values to be checked and successive rejection of those observed values which have the largest deviations from the analysed values.
- 5) Computation of an analysis “vector” for each analysis box by solving a linear system of equations, the left hand side matrix being the covariance matrix corresponding to all observed values accepted by the final quality control and the right hand side being the vector of observational increments.
- 6) Evaluation of analysis increments for all forecast model gridpoints by scalar multiplication of the proper analysis vector with a vector containing covariances between the observed values and the grid point quantity to be analysed.

The actual application of the analysis system for the different HIRLAM model versions in the operational setup is briefly described in Appendix A.

After an analysis has been made the model balance has been affected to some extent. As a consequence an initialization scheme is used prior to the start of the model forecast. The initialization (Källén, 1996) removes partly the gravity waves caused by the model imbalance after the analysis.

6. Diagnostic output

A number of special output parameters are produced in connection with the HIRLAM forecasts. These are closely related to some of the main forecast variables. The formulae associated with some key diagnostic parameters are given below.

6.1. Wind at 10 metre

The formulae used are derived by a vertical integration of basic formulae from boundary layer theory (Paulson, 1970; Businger et al., 1971). It is assumed that the diagnosed winds apply to a level between the surface and the height of the lowest model layer. For the unstable boundary layer we get for the wind component u in the west-east direction

$$\begin{aligned}
 u_{(Z)} = u_{(N)} - \frac{u_*}{k} & \left(- \ln \left(\frac{Z}{Z_N} \frac{(1 + X_N^2)}{(1 + X^2)} \right) - \right. \\
 & \left. 2 \ln \left(\frac{1 + X_N}{1 + X} \right) + 2 \left(\tan^{-1}(X_N) - \tan^{-1}(X) \right) \right) \quad (90)
 \end{aligned}$$

$$X = \left(1 - 15 \frac{Z}{L} \right)^{\frac{1}{4}}, \quad X_N = \left(1 - 15 \frac{Z_N}{L} \right)^{\frac{1}{4}}$$

k is the von Kármán constant, L is the Monin-Obukov length scale, u_* is the friction velocity. A similar formula applies to the wind component v in the northerly direction.

For the stable planetary boundary layer the following modified form of the integrated profiles is used in order to guarantee that the diagnosed wind speed is no larger than that provided by the lowest model layer wind.

$$u_{(Z)} = \frac{u_*}{k} \ln \left(\frac{Z}{Z_0} \right) + u_N \left[1 - \exp \left(- \frac{b_m}{k} \frac{u_*}{u_N} \frac{Z}{L} \right) \right] \quad (91)$$

A similar equation applies to v_Z . $b_m = 4.0$

6.2. Temperature and humidity at 2 metre

The equations for temperature and specific humidity are given below applying similar principles as mentioned above for the wind components (θ_* and q_* are the corresponding surface fluctuations for temperature and specific humidity, respectively) For the unstable boundary layer we get for the potential temperature (θ) and specific humidity (q):

$$\theta_{(Z)} = \theta_{(N)} - \frac{\theta_*}{k} \ln \left(\frac{Z_N}{Z} \frac{(1+Y)^2}{(1+Y_N)^2} \right) \quad (92)$$

$$q_{(Z)} = q_{(N)} - \frac{q_*}{k} \ln \left(\frac{Z_N}{Z} \frac{(1+Y)^2}{(1+Y_N)^2} \right) \quad (93)$$

$$Y = \sqrt{1 - 9 \frac{Z}{L}}, \quad Y_N = \sqrt{1 - 9 \frac{Z_N}{L}}$$

For the stable planetary boundary layer the corresponding equations are

$$\theta_{(Z)} = \theta_s + \frac{\theta_*}{k} \ln \left(\frac{Z}{Z_0} \right) + \Delta\theta_N \left[1 - \exp \left(- \frac{b_h}{k} \frac{\theta_*}{\theta_N} \frac{Z}{L} \right) \right] \quad (94)$$

$$q_{(Z)} = q_s + \frac{q_*}{k} \ln \left(\frac{Z}{Z_0} \right) + \Delta q_N \left[1 - \exp \left(- \frac{b_q}{k} \frac{q_*}{q_N} \frac{Z}{L} \right) \right] \quad (95)$$

Currently $b_h = b_q = b_m$, $\Delta\theta_N = \theta_N - \theta_s$, $\Delta q_N = q_N - q_s$.

6.3. Boundary layer height

A boundary layer height H_{pbl} which is useful for applications related to air pollution is computed diagnostically as an output field from parameters produced during the forecast

$$Ri_b = \frac{\frac{g}{\theta_{vs}} (\theta_{vh} - \theta_{vs}) (z_h - z_s)}{(u_h - u_s)^2 + (v_h - v_s)^2 + bu_*^2} \quad (96)$$

This equation (Vogelezang and Holtslag, 1996) is solved iteratively using a criterion that the bulk Richardson number Ri_b must not exceed a critical value. Subscripts 's' and 'h' denote the top of the surface layer ($z_s = 0.1h$) and the top of the boundary layer, respectively. Guided by sensitivity experiments Ri_b is set to 0.25 and $b=100$. $H_{pbl} = z_h$ when the critical value of the Richardson number is reached.

6.4. MSLP

Charts of mean sea level pressure (MSLP) are widely used in weather forecasting. An obvious problem exists in the case of high elevated ground. Traditionally a fictitious MSLP is estimated using near surface information on temperature and assumptions on a temperature lapse rate ‘below ground’ to estimate a reasonable MSLP as an extrapolation. This method, however, is quite sensitive to the assumptions made, in particular in the case of very high mountains. To minimize these problems, the vertical extrapolation is replaced by investigating a horizontal variation. This method has been described in the literature (Pielke and Cram, 1987).

The diagnosed values P_{msl} of a non-divergent surface MSLP, is obtained from a Poisson equation

$$\frac{\partial^2 P_{msl}}{\partial x^2} + \frac{\partial^2 P_{msl}}{\partial y^2} = \frac{\partial}{\partial x} \left(\frac{(v_g f)}{\theta} \right) - \frac{\partial}{\partial y} \left(\frac{(u_g f)}{\theta} \right) \quad (97)$$

In the equation above u_g and v_g are geostrophic wind components and f is the Coriolis parameter. The relationship has been derived by taking the curl of the expressions below for the surface geostrophic winds.

$$v_g = \frac{\theta}{f} \frac{\partial \tilde{P}_s}{\partial x} + \frac{g}{f} \frac{\partial z_g}{\partial x} = \frac{\theta}{f} \frac{\partial P_{msl}}{\partial x} \quad (98)$$

$$u_g = -\frac{\theta}{f} \frac{\partial \tilde{P}_s}{\partial y} - \frac{g}{f} \frac{\partial z_g}{\partial y} = -\frac{\theta}{f} \frac{\partial P_{msl}}{\partial y} \quad (99)$$

In the expressions above z_g is the height of the ground above mean sea level, and

$$\tilde{P}_s = c_p \left(\frac{p}{p_0} \right)^{\frac{R}{c_p}}, \quad p_0 = 1000 \text{ hPa.}$$

In order to solve the Poisson equation (97) it is necessary to compute the potential temperature θ . Also the lateral boundary values of P_{msl} are needed. These are supplied by a traditional extrapolation procedure. Otherwise a solution of the Poisson equation is sufficient to derive the diagnosed (non-divergent) MSLP in the internal model area. The solution is found by a traditional relaxation method.

Appendix A. DMI model setup (October 1999)

The operational HIRLAM system is run on an NEC-SX4 supercomputer with 16 processors and a peak performance of 32 Gflops (See figure 3). The lateral boundary values and observations are received on an 8 processor ORIGIN 200 computer. Boundary values from ECMWF (European Centre for Medium-Range Weather Forecasts) are received twice a day. The GTS messages are processed and encoded to BUFR format. The SGI ORIGIN computer also contains an operational database with files produced by the operational runs. The computationally demanding operations take place on an NEC-SX4 supercomputer (analyses and forecasts). The produced model level files are archived on a mass storage device.

The operational system consists of several nested models named ‘DMI-HIRLAM-G’, ‘DMI-HIRLAM-N’, ‘DMI-HIRLAM-E’ and ‘DMI-HIRLAM-D’, respectively. In short, the models are often abbreviated by the letters ‘G’, ‘N’, ‘E’ and ‘D’, respectively. The model integration areas are shown in figure 4 below.

The system setup with respect to resolution, time step, boundaries and data assimilation is illustrated in table 1. The boundary files of model ‘G’ are always the latest available from ECMWF. The model ‘G’ provides the lateral boundaries of models ‘N’ and ‘E’. Finally, model ‘E’ supplies the boundaries for the very high resolution model ‘D’ around Denmark. The most important products from an operational point of view are produced by the high resolution models ‘E’ (for the European area), ‘D’ (for the Danish area) and ‘N’ for Greenland. The boundary age 0 h* in table 1 means that 6 hours old model ‘G’ boundary values actually are used in the long forecasts from 06 UTC and 18 UTC. Also a 1 hour boundary update cycle is used (se ‘1/(3h)*’ in table 1).

A special data-assimilation feature applies to DMI-HIRLAM-G. At about 11 UTC the assimilation is restarted from the interpolated operational analysis provided by the

Table 1: Important parameters describing the operational HIRLAM models at DMI (*: see text).

Model Identification	G	N	E	D
grid points (mlon)	202	194	272	182
grid points (mlat)	190	210	282	170
No. of vertical levels	31	31	31	31
horizontal resolution	0.45°	0.15°	0.15°	0.05°
time step (dynamics)	240 s	100 s	100 s	36 s
time step (physics)	720 s	300 s	300 s	108 s
host model	ECMWF	G	G	E
boundary age	12 h	0 h	0 h*	0 h
boundary update cycle	1/(6h)	1/(1h)	1/(3h)*	1/(1h)
data assimilation cycle	3h	6h	3h	6h
forecast length (long)	60h	36h	48h	36h
long forecasts per day	2	2	4	2

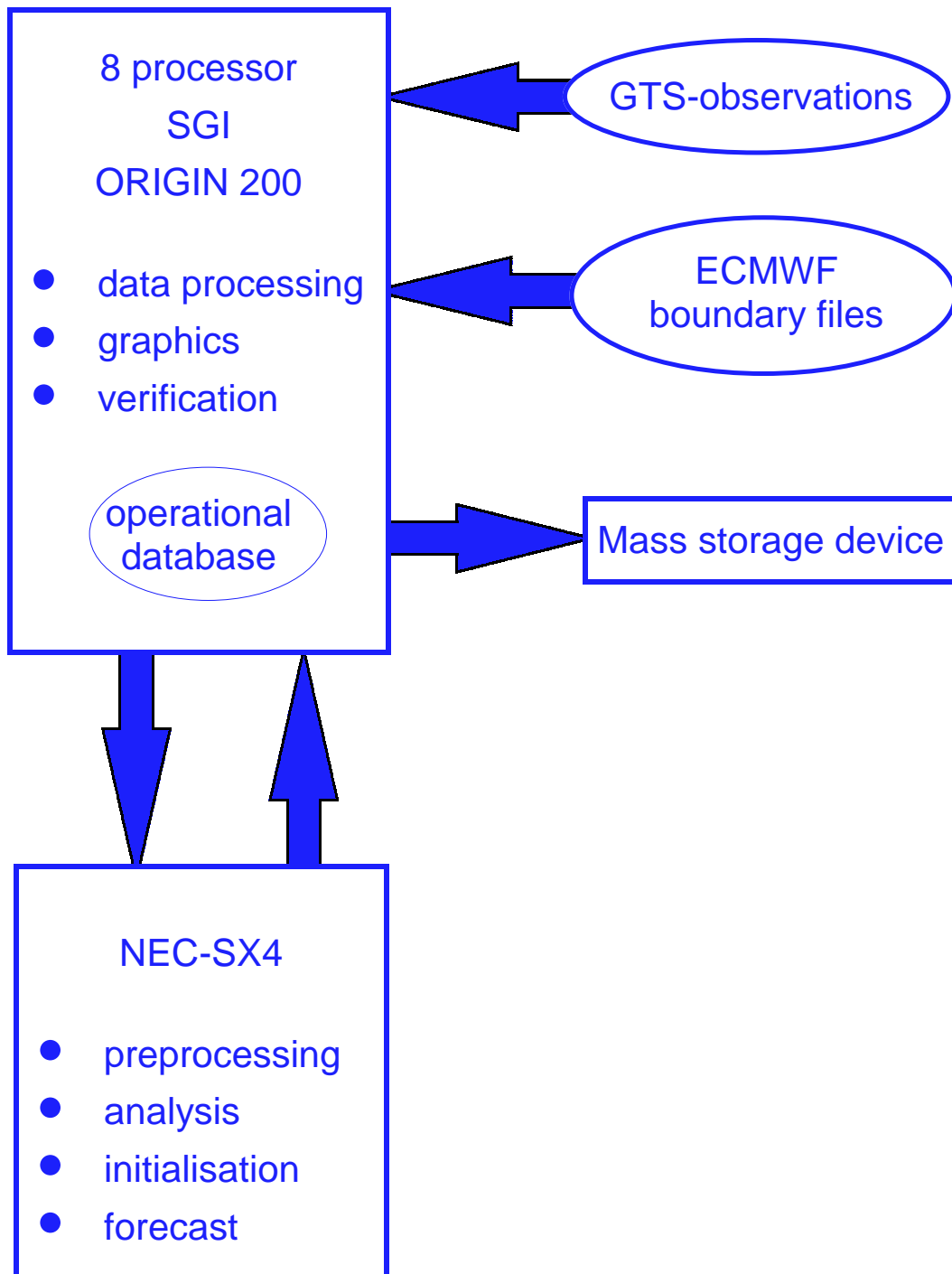


Figure 3: Computers and data flows

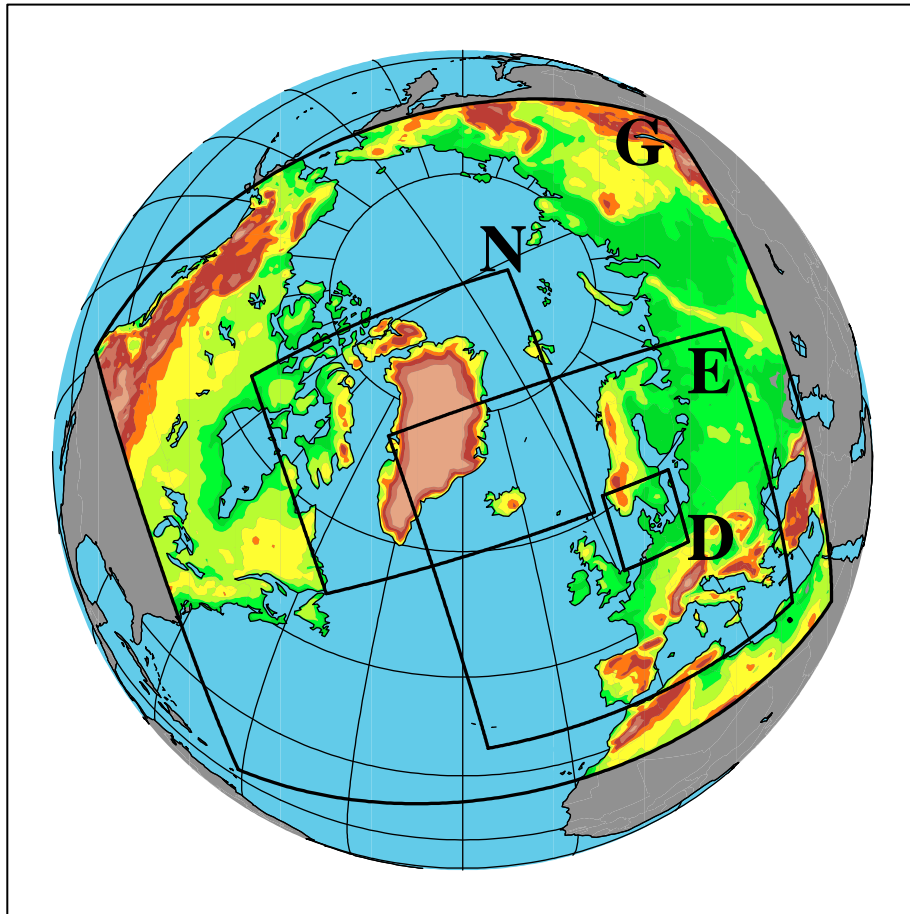


Figure 4: The DMI operational model integration areas.

ECMWF model at 00 UTC initial time. However, there is not full weight given to the ECMWF field values. The following vertical weighting is used.

$$\gamma_{hir}^* = (p/p_s)^2 \gamma_{hir} + \left(1 - (p/p_s)^2\right) \gamma_{ecm} \quad (100)$$

In (100) p is pressure, p_s is surface pressure, γ_{hir}^* is the adjusted HIRLAM value while γ_{hir} and γ_{ecm} are the uncorrected values from HIRLAM and from ECMWF, respectively. The reason for the restart is the current situation that more data have been available to the ECMWF analysis over the Atlantic region, with the effect that the largest atmospheric scales are often analysed better with the ECMWF data assimilation system. A vertical weighting is used because it is considered important to retain the HIRLAM model specific features close to the ground. Subsequently a 3-hourly assimilation cycle is run (from 00 UTC) until 09 UTC. The model output is averaged over a period of $\pm M$ minutes around the valid output time, in order to avoid the risk of short period fluctuations in the case of short time steps. Currently $M = 15$ minutes is used. A similar restart procedure is initiated in the evening from 12 UTC ECMWF analyses.

The other models run their own data assimilation using the HIRLAM data assimilation system and forecast model. The run schedule is shown in table 2.

Table 2: Operational time schedule. G_E denotes restart from ECMWF analysis. See text.

UTC	G	N	E	D
1:40	G00+48h			
1:50			E00+48h	
2:05				D00+36h
2:45	G00+60h			
2:55		N00+36h		
ECMWF 00 UTC				
7:40			E06+48h	
10:00	G_E00+03h G03+03h G06+06h G09+03h			
10:10			E03+03h E06+06h E09+03h	
10:20				D06+06h
10:25		N06+06h		
13:40	G12+48h			
13:50			E12+48h	
14:05				D12+36h
14:45	G12+60h			
14:55		N12+36h		
19:40			E18+48h	
ECMWF 12 UTC				
22:45	G_E12+03h G15+03h G18+06h G21+03h			
22:55			E03+03h E06+06h E09+03h	
23:05				D06+06h
23:10		N06+06h		

Appendix B. Grid used for horizontal discretization

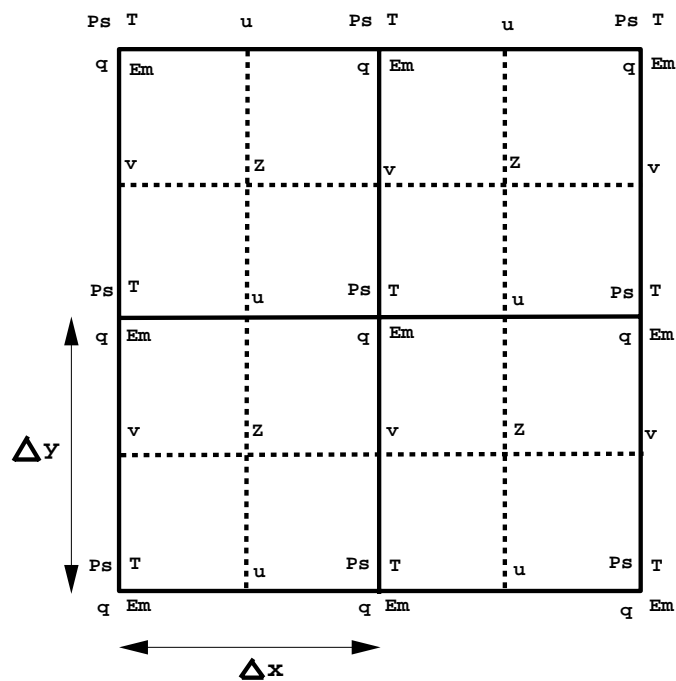


Figure 5: Arrangement of variables in Arakawa C grid. P_s is surface pressure, T is temperature, q is specific humidity (moisture variable), E_m is kinetic energy, u, v are horizontal wind components, Z is absolute vorticity.

Appendix C. Computational details of longwave radiation

$$\left(\frac{\partial T}{\partial t}\right)_i = \left(\frac{\partial T}{\partial t}\right)_{i1a} + \left(\frac{\partial T}{\partial t}\right)_{i2a} + \left(\frac{\partial T}{\partial t}\right)_{i1c} + \left(\frac{\partial T}{\partial t}\right)_{i2c} \quad (101)$$

$$\left(\frac{\partial T}{\partial t}\right)_{i1a} = W_1(R_1 + R_2 + R_3) \quad (102)$$

$$\left(\frac{\partial T}{\partial t}\right)_{i2a} = W_2\zeta_2(R_1 + R_3) + (W_2 - W_3)R_2 \quad (103)$$

$$\left(\frac{\partial T}{\partial t}\right)_{i1c} = W_4R_4 + W_5R_5 + W_6R_6 \quad (104)$$

$$\left(\frac{\partial T}{\partial t}\right)_{i2c} = W_7R_7 + W_8R_5 + W_9R_6 \quad (105)$$

R_1, \dots, R_7 are given in finite difference form below

$$\begin{aligned} R_1 &= B(T_k)[e(0, p_{k-\frac{1}{2}}) - e(0, p_{k+\frac{1}{2}})] \frac{g}{c_p \Delta p_k} \\ R_2 &= [B(T_{e0}) - B(T_k)][e(p_{k-\frac{1}{2}}, p_s) - e(p_{k+\frac{1}{2}}, p_s)] \frac{g}{c_p \Delta p_k} \\ R_3 &= -a_6 q_k^3 - a_7 \\ R_4 &= [-B(T_{k-\frac{1}{2}}) + B(T_{k-1})e(0, p_{k-\frac{1}{2}}) + a_9 - \zeta_3 + a_{10}\sqrt{q_{k-1}} + a_{11}q_{k-1}] \frac{g}{c_p \Delta p_k} \\ R_5 &= [B(T_{l*}) - B(T_{k+\frac{1}{2}})][\zeta_4 + G_{k+1}(1 - \zeta_4)] \frac{g}{c_p \Delta p_k} \\ R_6 &= [B(T_{e0}) - B(T_{k+\frac{1}{2}})][\zeta_5 + G_{k+1}(1 - \zeta_5)] \frac{g}{c_p \Delta p_k} \\ R_7 &= [B(T_{h*}) - B(T_{k-\frac{1}{2}})][\zeta_6 + G_{k-1}(1 - \zeta_6)] \frac{g}{c_p \Delta p_k} \\ G_j &= \frac{1}{1 + a_{13} \frac{(\Delta \epsilon)}{(\Delta p)^j}}, \quad 1 \leq j \leq N \end{aligned} \quad (106)$$

The customary assumption is applied, that ‘‘grey’’ clouds may be introduced by reducing the normal grid box fractional cloud cover f with the cloud emissivity according to (107):

$$f_e = f[1 - \exp(-\zeta_1 M)] \quad (107)$$

The parameter ζ_1 depends on cloud type. It varies linearly with the vertical coordinate.

$$\zeta_1 = \max\left(0.05 + 0.20 \frac{(\eta - \eta_1)}{1 - \eta_1}, 0.05\right), \quad \eta_1 = 0.25$$

M is the vertically integrated cloud condensate (g/m^2) in the cloud. The radiative impact of cloud layers above are taken into account by computing radiation from a maximum effective cloud cover f_{eh*} . In order to treat high vertical resolutions in a

realistic way this maximum effective cloud cover is determined in the following way: For any level above the layer in consideration and effective cloud cover is assigned by (107) using local values of cloud cover and ζ_1 while M is determined as the vertical integral of cloud condensate up to the top atmospheric model layer. The maximum of these effective cloud covers is f_{eh*} which is assigned to the level where the maximum occurs. A similar computation is carried out for the maximum effective cloud cover f_{el*} for clouds below the layer considered. Also the effect of the cloud covers f_{eh} and f_{el} of the neighbouring layers above and below, respectively, is taken into account by assuming zero net flux contribution at the intersection of overlapping clouds.

$$\begin{aligned}\zeta_2 &= \min\left(\frac{p_{k-\frac{1}{2}} - p_{h*}}{a_8}, 1\right) \\ \zeta_3 &= a_{12} \frac{(1 - \eta)}{(1 - \eta_0)}, \quad \eta_0 = 0.05 \\ \zeta_4 &= \min\left(\frac{a_{14}}{p_{l*} - p_{k+\frac{1}{2}}}, 1\right) \\ \zeta_5 &= \min\left(\frac{a_{14}}{p_s - p_{k+\frac{1}{2}}}, 1\right) \\ \zeta_6 &= \min\left(\frac{a_{14}}{p_{k-\frac{1}{2}} - p_{h*}}, 1\right)\end{aligned}$$

$B(T_j)$ is the Planck black body radiation at temperature T_j . R_1 is the “cooling to space” term, and R_2 accounts for the radiative effect of ground radiating with an effective temperature T_{e0} . The first term in R_3 represents crudely the effect of cooling due to water vapour continuum which is of major importance only in a moist and warm atmosphere (Savijärvi, 1990). The cooling due to other gases like CO_2 and O_3 seems to be rather small and fairly constant in the troposphere (Liou, 1980; Paltridge and Platt, 1976). Hence a constant cooling term a_7 is introduced to represent this.

The factor ζ_2 in (103) represents reduced cooling below clouds. Paltridge and Platt (1976) note that the assumption of zero cooling below clouds might be compatible with a “cooling to space” approximation. However, this assumption appears to be too drastic (Sass et al., 1994). Instead the cooling rate is assumed to vary linearly with a pressure increment below cloud, from zero to a value valid for ‘clear air’, through a certain depth a_8 . The last term in (103) proportional to $W_2 - W_3$ represents the effect of radiation from the ground attenuated by overlapping low level clouds.

In (104) the first term estimates the net radiation balance at cloud top. The downward radiation due to gases other than water vapour including aerosols is described by $a_9 - \zeta_3$ taking into account a flux correction associated with the integrated cooling in clear air due to these constituents. The terms involving a_{10} and a_{11} parameterizes an additional flux due to water vapour continuum.

The additional terms in (104) and (105) involve a determination of effective radiation temperatures describing radiative interaction either between clouds or between ground and cloud. The first brackets in the formulations of R_5, R_6 and R_7 involving differences

between related Planck-functions is multiplied by a factor between 0 and 1 according to the expression in the second brackets. An empirical function G_j expressing sensitivity to the emissivity slope for clear air next to the cloud has been introduced (106). From a qualitative point of view it is obvious that the level of an effective radiation temperature for upward radiation comes closer to the ground as the humidity below cloud base decreases. In the extreme (unrealistic) situation of no absorption in the clear atmosphere the formulation automatically guarantees transmission of radiation between ground and cloud without attenuation.

W_1, \dots, W_9 are weight functions related to the cloud overlap assumption.

$$W_1 = 1 - \max(f_e, f_{eh*})$$

$$W_2 = \max(f_{eh*} - f_e, 0)$$

$$W_3 = \min(\max(f_{el*} - f_e, 0), W_2)$$

$$W_4 = \max(f_e - f_{eh*}, 0)$$

$$W_5 = \max(\min(f_{el*}, f_e) - f_{eh*}, 0) - \max(\min(f_{el}, f_e) - f_{eh*}, 0)$$

$$W_6 = W_4 - \max(\min(f_{el*}, f_e) - f_{eh*}, 0)$$

$$W_7 = \max(\min(f_{eh*}, f_e) - f_{eh}, 0)$$

$$W_8 = \max(\min(\min(f_{el*}, f_e), f_{eh*}) - f_{el}, 0)$$

$$W_9 = \min(f_{eh*}, f_e) - \min(\min(f_{el*}, f_e), f_{eh*})$$

Values of constants

$a_1 = 0.60$	$a_2 = 0.17$	$a_3 = 0.0082$
$a_4 = 0.0045$	$a_5 = 0.4343$	$a_6 = 11.5 \frac{\text{K}}{\text{s}}$
$a_7 = 2.3 \cdot 10^{-6} \frac{\text{K}}{\text{s}}$	$a_8 = 7 \cdot 10^4 \text{ Pa}$	$a_9 = 35 \frac{\text{J}}{\text{m}^2 \text{ s}}$
$a_{10} = 250 \frac{\text{J}}{\text{m}^2 \text{ s}}$	$a_{11} = 750 \frac{\text{J}}{\text{m}^2}$	$a_{12} = 24 \frac{\text{J}}{\text{m}^2 \text{ s}}$
$a_{13} = 2 \cdot 10^4 \text{ Pa}$	$a_{14} = 2.5 \cdot 10^3 \text{ Pa}$	$a_{15} = a_{14}$
$b_1 = 1.67$	$b_2 = 1.7 \cdot 10^{-6} \frac{\text{K}}{\text{s}}$	$b_3 = 0.03$
$b_4 = 0.05$	$b_5 = 1.20$	$b_6 = 1.25$
$b_7 = 0.013$	$b_8 = 1.4$	$b_9 = 0.10 \frac{\text{m}^2}{\text{g}}$
$b_{10} = 40$	$b_{11} = 0.5$	$b_{12} = 0.8$

Stefan Boltzmann's constant $\sigma = 5.67 \cdot 10^{-8} \frac{\text{J}}{\text{m}^2 \text{K}^4 \text{ s}}$

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